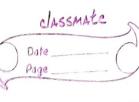
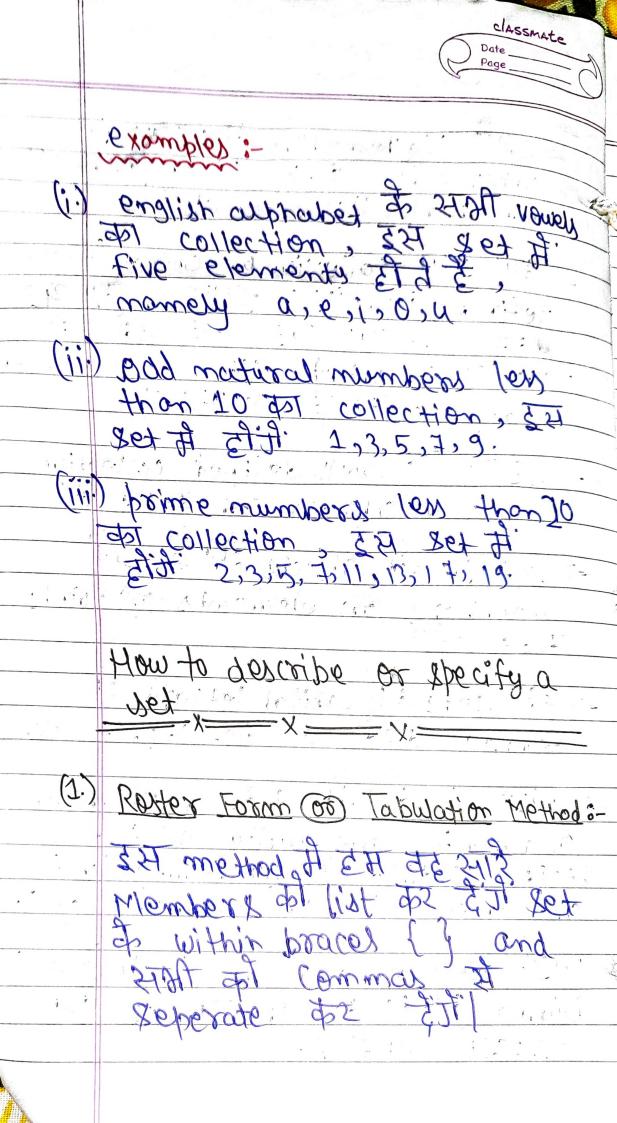
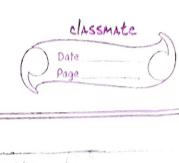
Set Theory



Universe H Eld & The living 21 mon-living 25 object & > दिया गया collection of Object well-प्रकार कहानाएगा। उत्पार, हम यह प्रकार निर्मा किंद्रिक की की की किंद्रिक की किंद्रिक की की किंद्रिक की की किंद्रिक > SET: Cos well defined collection of objectional and a > Set H and Objects Eld & 30 g members or elements or paints denote doit à i.e. A, B, (.--etc. > 3012 Allo ml a is on element of a set A, we write a E A, fit start of A a is an element of A. SATIT OF Element Set A HOTEL belong of TIE A 32 EH DA EN DA EN DA





Example

(1) A = 8et of all factors of 24 $A = \{1, 2, 3, 4, 6, 8, 12, 24\}$

(ii) B= set of law prime mumbers between 50 and 70

: B= { 53,59,61,67}

(iii) C= set of all integers between - 3 and 110 minutes and 1

 $: C = \{-1, 0, 1, 2, 3, 4, 5\}$

Note: N: Set of all matural numbers.

Z: Set of all integers.

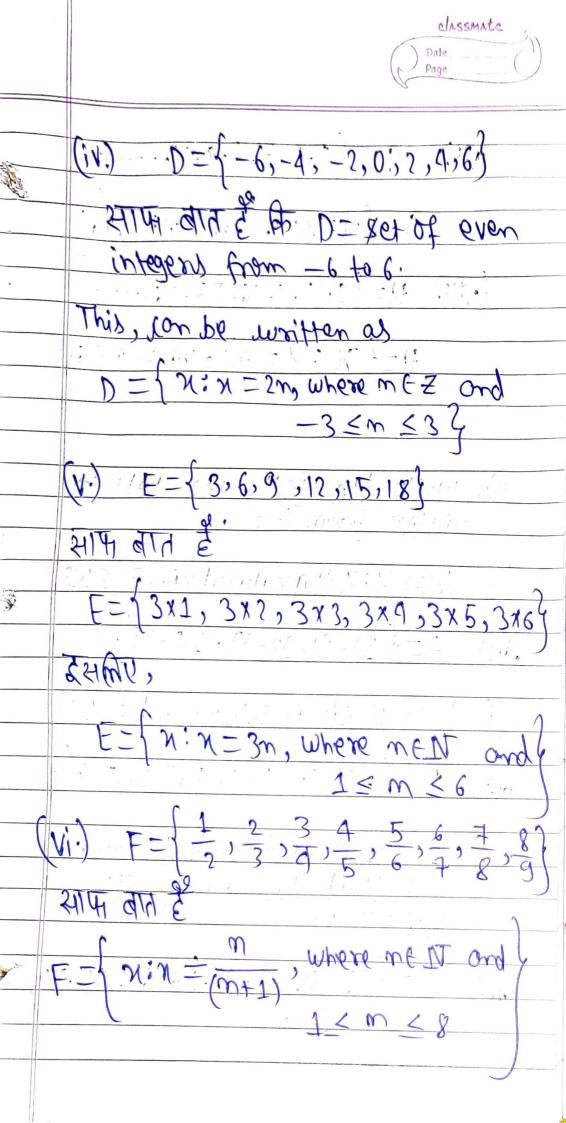
Q: Set of all rational numbers

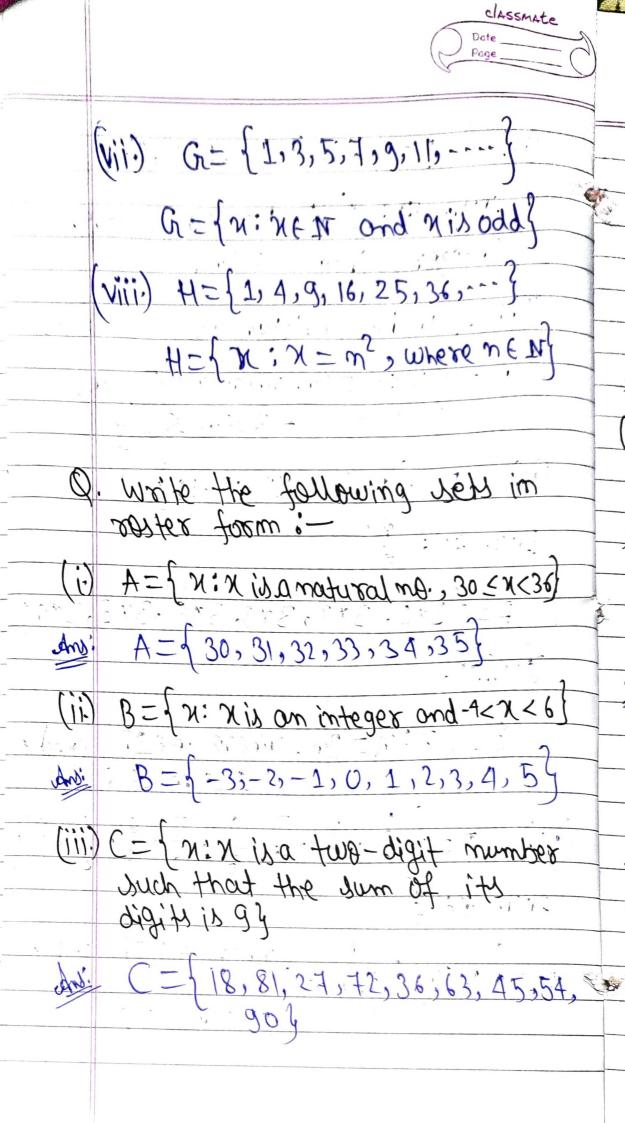
R: Set of all real numbers.

(2) Set - Builder Form:

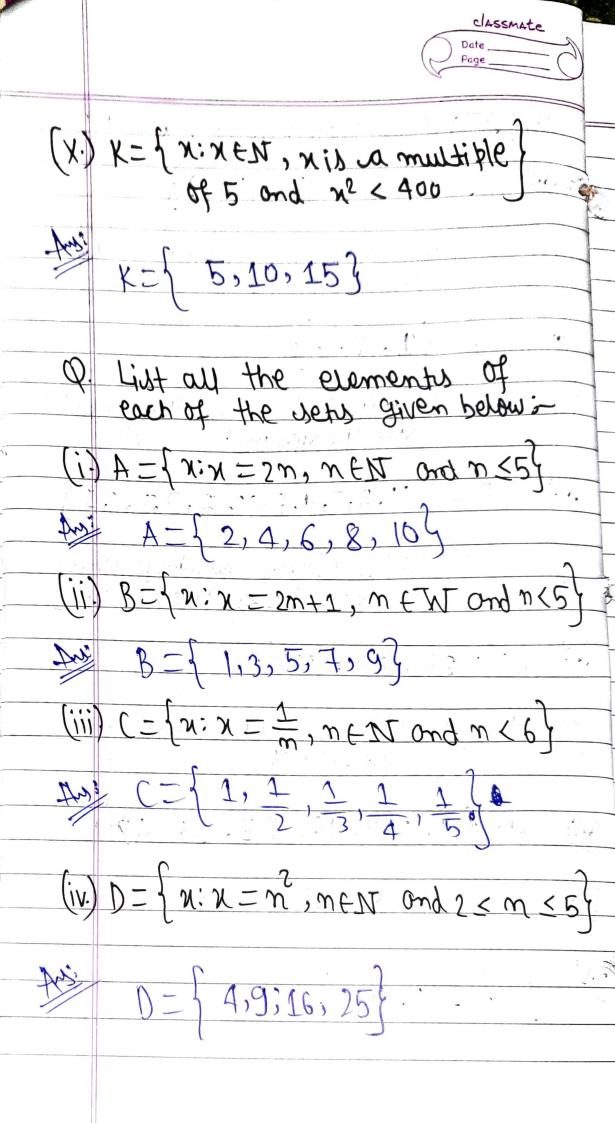
27 Method HEH de property list 27 properties of set of e2 element Satisfy open 2 32 list open 21

, रिहिला मञ् Ju: n has properties p3. -: रिर्डिंग मिड्ड मिड the set of all those x such that each x such that (i) A={1,2,3,40,5,6,74... Combe written as A={N:NEW and N<8} B={1,2,4,7,14,28} B= { N: NEN and xisa factor Can be written as 2,4,8,16,323. con be written as C= Jx: x = 2, where mEN ond





classmate (iv) D={x:x is on integer, 2 <9} $D = \{-3, -2, -1, 0, 1, 2, 3\}$ (V) E={x:x is a prime no; which is a y divisor of 42. ship E= 1, 3, 74 VI) F= { X: X is a letter in the word "MATHEMATICS" $F = \{M, A, T, H, E, M, A, T, I, G, S, C, S, C,$ (Vii) G= { x:xis a frime number on and G= 83,89,974 (viii) H= {21:x is a perfect square and dri H= {1, 1, 9, 16, 25, 36, 49} (ix) J= 1x: x ∈ R and x2+x-12=0 J= 1-4,3: 1:11.



(V)
$$E=\{x: x \in Z \text{ and } x^2 = X\}$$

$$E=\{0,1\}$$

(i)
$$A = \{1, \frac{1}{4}, \frac{1}{9}, \frac{1}{16}, \frac{1}{25}, \frac{1}{36}, \frac{1}{49}\}$$

$$A = \left\{ \begin{array}{ll} \text{N: } \chi \in = \frac{1}{m^2}, \text{ m \in } N \text{ . cond } 1 < m < 7 \right\} \\ \text{(ii.)} \quad B = \left\{ \begin{array}{ll} 1, \frac{2}{2}, \frac{3}{5}, \frac{4}{10}, \frac{5}{17}, \frac{6}{26}, \frac{7}{37}, \frac{7}{50} \right\} \end{array}$$

And:
$$B = \{ x; y = \frac{m}{(n^2+1)}, m \in \mathbb{N} \text{ and } 1 \leq m \leq 7 \}$$

$$(N) D = \{-1,1\}$$

$$A = \{n: n \in \mathbb{Z}, n^2 = 1\}$$

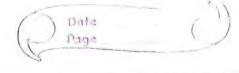
(V) E= {n:n= 7n,nen, 2≤n≤14} As: E= {19,21,28,35, 12,....,98} Some Terms Related to Sets Vab ऐसा प्रश्न कीर्ड भी element मही ही। At doch tell set or void set Example: (i) {N: N E M and 2 < N < 3 4 = 0, since there is no matural number lying between 2 and 3. (ii) [x:xis a number, x \pi x)=0. wince there is no number which is not equal to itself. (11:) \n: x EN, x < 5 and x 77 = 0, wince there is no natural no. which is less than 5 and greater than I.

Singleton Set:
272 Vos VAI set Etal & CARA (2) 4

Vos element Etal! Example: (i) (o) is a singleton set whose Only element is 0. (ii) { 15} is a singleton set unose only element is 15. (iii.) [-8] is a singleton set whose only element is -8. 4 Finite Set & Infinite Sets The empty (21) mon-empty set till monof elements for counting the end 42 31 counting finite set of finite set of Et 2327 infinite set of E The mo- of distinct elements contained in a finite bet A is denoted by m(A).

clasemate

examples of finite set: -(c) A={2,4,6,8,10,125 साम है की A एक finite set है क्योंकी m(A)=6 11.) B= set of all detters in the English Alphabet स्माप्त है की है एक संगंध अहर है m(B) - 26(iii) C= { x: x & Z, s and x2-36=0 9 साम है की (= १-6, 6), नी की Va finik det Z. Frish examples of infinite set: (i) The set of all points on the arc of a xixcle is on infinite set (ii) The set of all points on a line Jegment is on infinite set (iii) The set of all straight lines parall to a given line, day the n-axis is on infinite set



= Feach of the sels N; Z', Q and R is an infinite set.

NOTE: - All infinite vets connet be described in roster form.

* Equal Set: -

exactly same elements of ond we write, A = B.

नहीं तो sets unequal है अर्थि हम

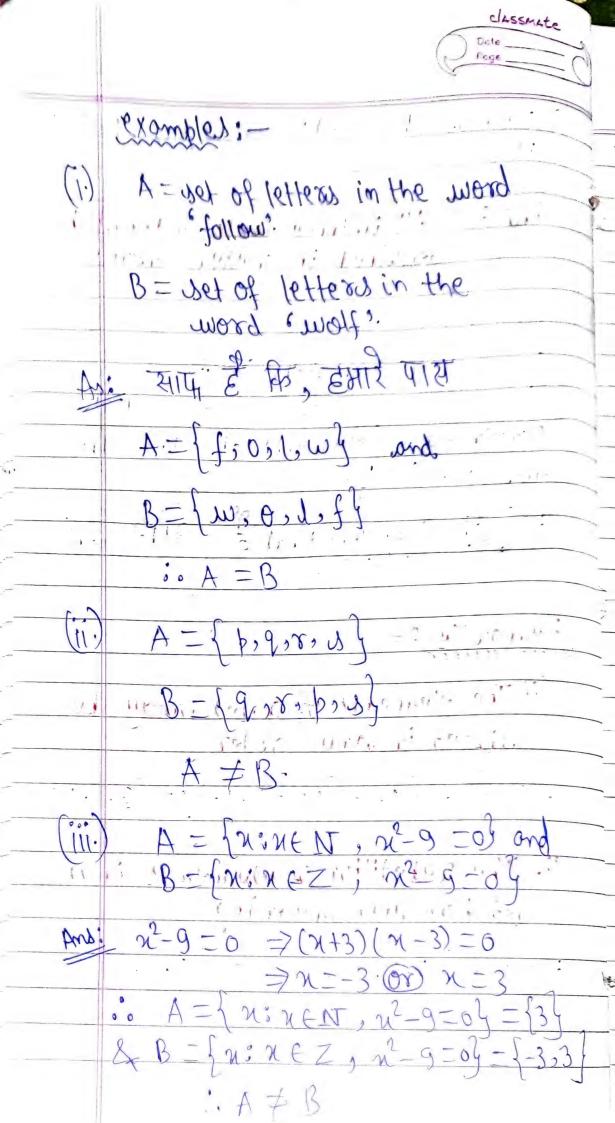
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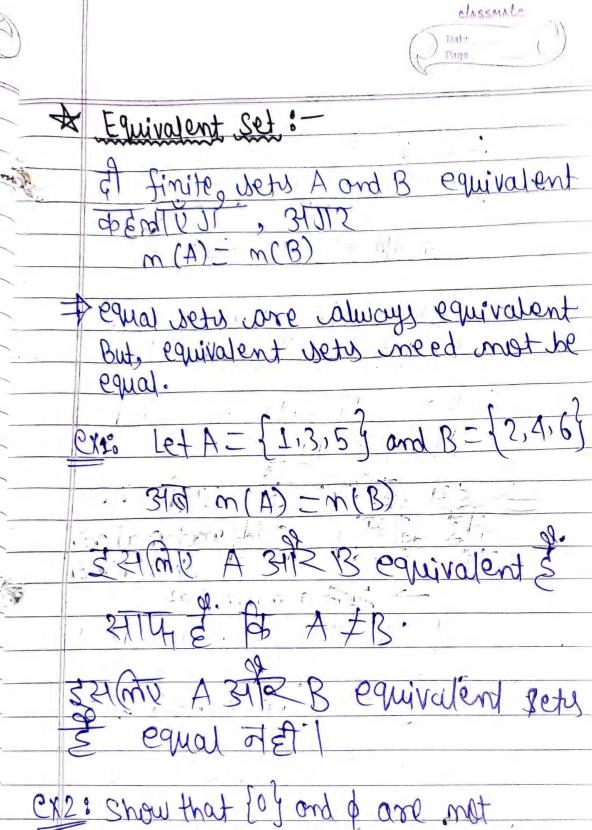
(i) The elements of a set may be sisted in any order

तीरी की, [1,2,3]= [2,1,3]= [3,2,1]

(ii) The repetition of elements in a yet true meaning.

32 + 31, 1, 1, 2, 2, 3 = $\{1, 2, 3\}$

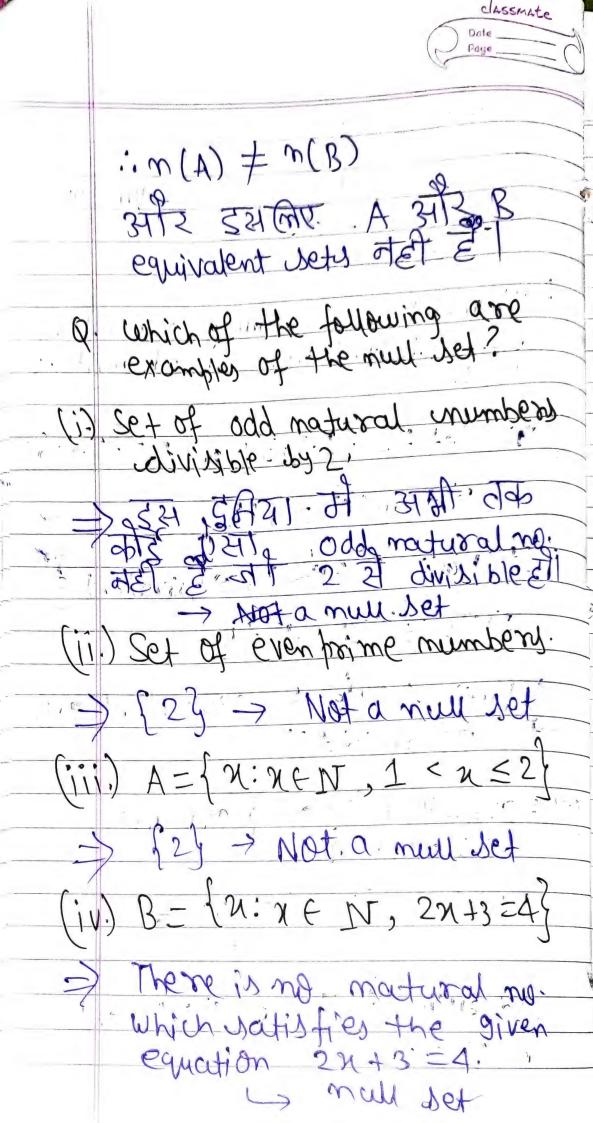




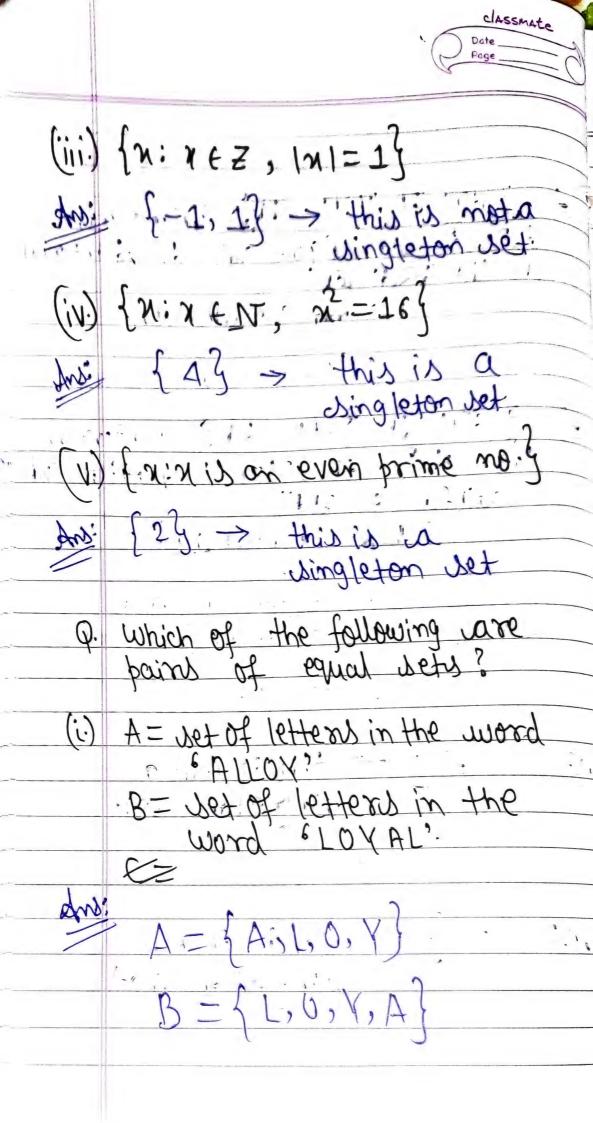
equivalent sets.

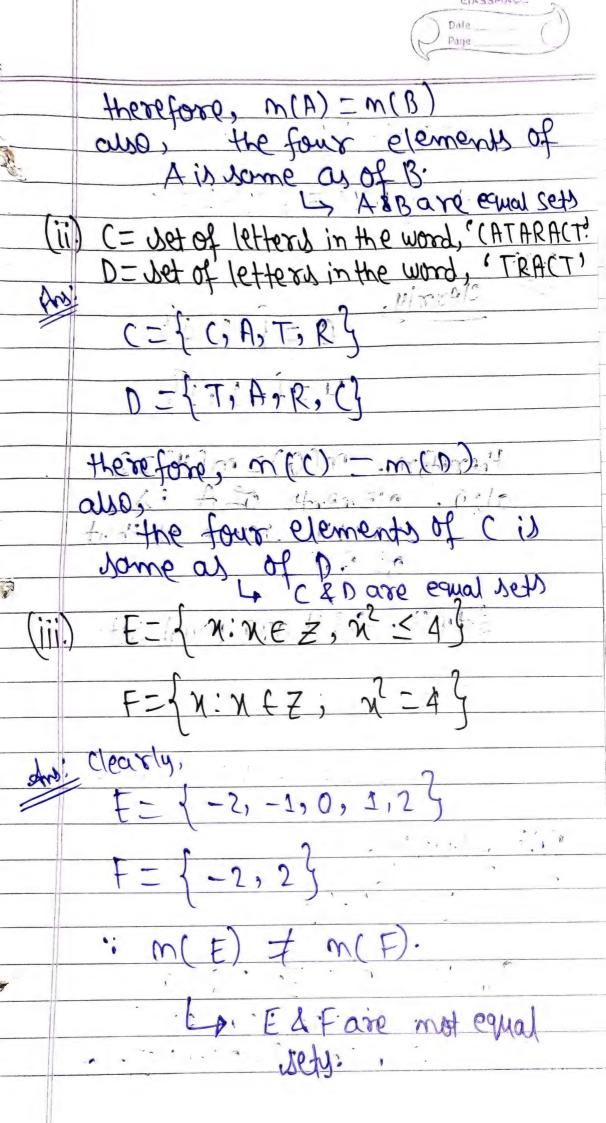
मान लिया कि A=101 &

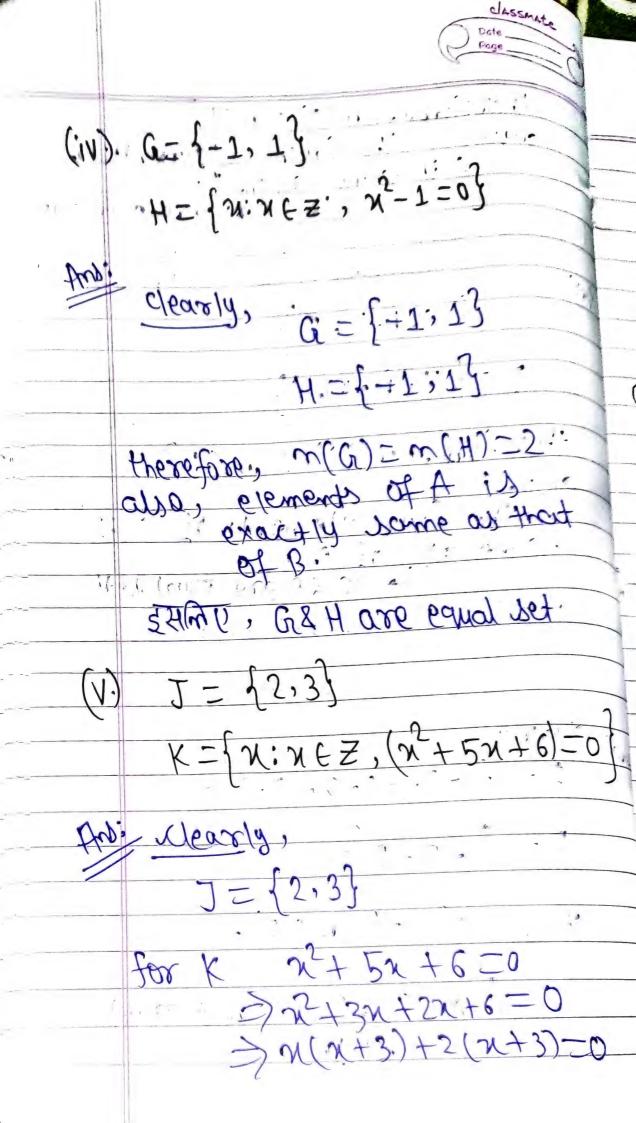
310, 21 H & A. m(A) = 1 and m(B) - (1.



(v.) C={N: N is prime, 90< N < 96} ने दुनिशा में ऐसा कोर्ट brime no... विस्ता है। स्ती (90, 96) के sinterval + 192 hum a mul set. (Vi) D= 1 X X ENT , 2+1 = 0 (iV) => 3 A21 A 1821 == ratural, No. 72 == 12 22 == 000 == 1 a null set Q. Which of the following are examples of the singleton set? i) [x:x EZ, x=4] Ans: {-2,2} -> this is most a singleton set (ii) \n: x EZ, x + 5 = 0 Ans: {-5} -> 30 it is a singleton bet







=> (x+3)(x+2)=0. $K = \{-3, -2\}$ 324 me , J & K are not equal 764. Q. Which of the following are pairs of equivalent sets? (i) A = {-2,-1,0} and B= {1,2,3} A&B some equivalent set. S (ii) C={x: x+E.N.; x<3}. and D={ 7: NEW , N<3}. Hodi clearly, C= {1,2,3} D={0,1,2,3}: $m(\mathbf{E}) = 3$ $m(\mathbf{D}) := 4$: m(0) = m(D) (& D are not equivalent set.

(iii) E={a,e,i,0,u} and F={p,q,r,s,t} U(E)= W(E)=2. E&F are equivalent set. Q. State whether the given set is finite or infinite: (i) A= bet of all triangles in a plane. the Est 64 plane 15 Byly Al mumbers of frangle got Etal & Elmit A is infinite set (ii) B = bet of all paints on the circumference of a circle Ans Circle do Circumférance 42 Poblot Als numbers of points et 21 21 21 21 Bis infinite set

(iii) (= set of all limes parallel to the y-oxis. र्य सकती है किश्वासी infinite lines to cid infinite det iv) D= set of all leaves on a tree. किसी भावाय प्राच पड़े हैं अपिनेपक (11) 11= 106 : तेड विश्वय तेड हैं अपिनेपक Dis infinite set E= bet of all positive integers, greater than 500. integers 37 old (infinite)

Sub Sets Subjet:

Subjet:

Subjet:

Subjet:

Subjet:

Set A dot 22

Set A dot 27

Set A dot 27 element set Boot aff

Element set Boot aff

A Superdet 3412 A CB 31 Proper Subset A # B det A det

do Est Subset of B

A CB. Supervet: 37172 A CB da Remark: 3-1012, Potes wingle element 2 At A At E B At Nubuet alet Elitt 29.1. 3412 341 (A) At I

examples of subsets (I) A={2,3,5} & B={2,3,5,7,9}. : A S B but A & B. 24 AU A is a proper susset of set B, i.e. ACB: B={2,3,5} 34d 1.EA MADO 18. 218 147 3 EB MEDOT 3 & A. BAA Thus A &B and B &A! 3) NCWCZ CQCR $N = \{1, 2, 3, 4 - - 3\}$ $W = \{0, 1, 2, - - - 3\}$ $Z = \{---2, -1, 0, 1, 2, 3, 4 - - 3\}$ $Q = \{N: Nisa mb. of form q, p, q \in R\}$ 1R = (-∞, ∞) xlearly NCW CZCQCR.

Then, which of the following statements is true? (i) {2,3} EA (b) {2,3} CA Rectify the wrong statement.

HILL & Bo A Uto Set of S.

HILL of 2133 & 4. (i) [2,3] EA is a true Statement (b) [2,39=CA is wrong. दसकी अगार ग्रहमको सही व {{2,3}} CA as tous Statement.

classmate Some results on subsets: Every set is a wabset of कहने का सत्ताल यह है कि हर set खुद का subset होता है। 2) The empty set is a subset of every set i.e. $\phi \subset A$ कहते का सतलाल अह है कि के या जी रिया set तस्त्री कोई element जहीं होता वह के सभी set की subset The total innumber of Jubilets of a set containing in elements िक्कि के साथ समसी :-HIN MUT of A Parafinite bet & ms. of Jubsets of A each containing no clement = m(0

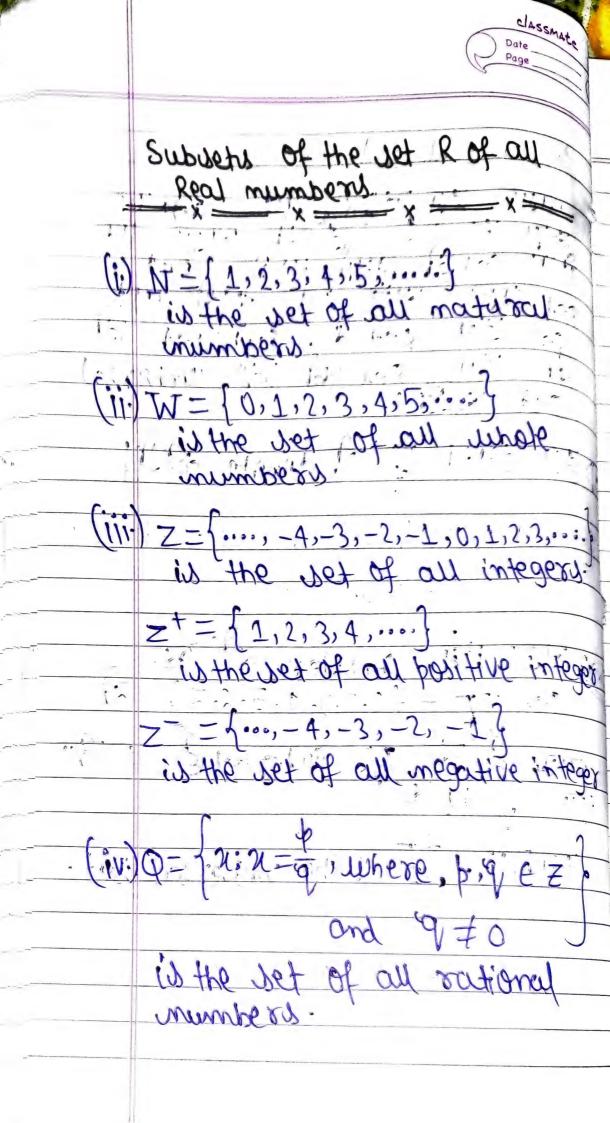
mo. of subsets of A each containing

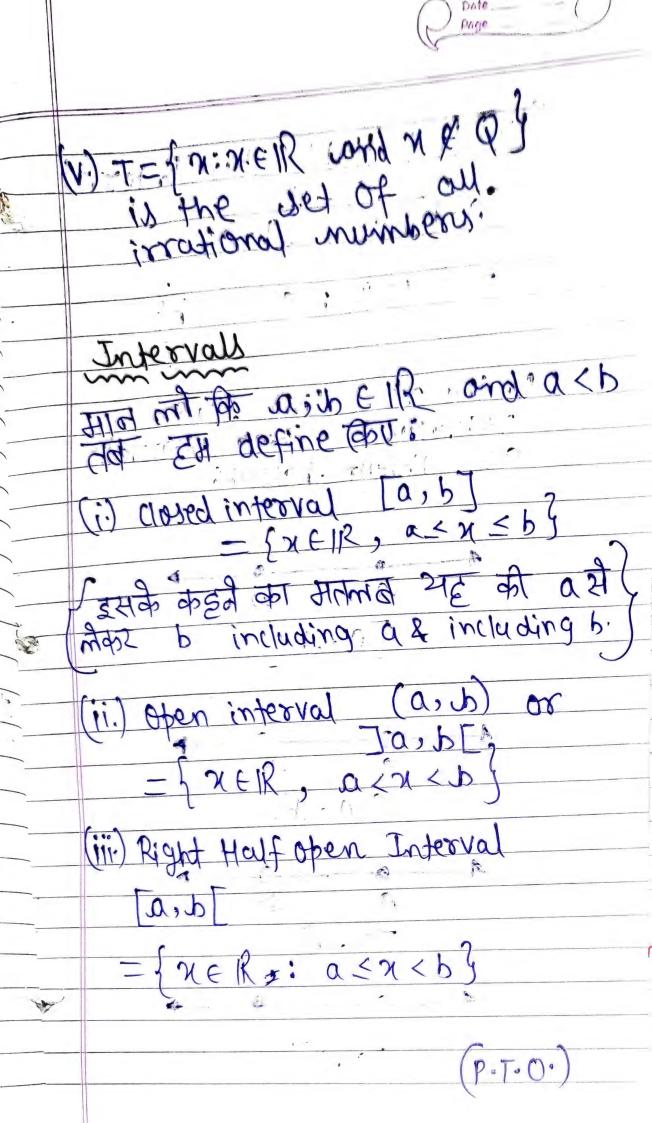
1 element

= mc mo of subsets of A each wondaining 2 elements : Total number of subsets of A. knowledge &

Classmate Page (

* Universal Set:-अगार हम बहुत होते हिंदी पर काम केट रहे ते ती अगार एक प्रभा अस्म जार्थ या अपार प्रभा अस्म जार्थ या कामी सार प्रभा उस इस की ट्रम. Universal Set कहा पर Rest stand to I Take HE Q: Let A={1,2,3}, B={2,3,4,5} 8ey II = {1,2,3,4,5,6,7} हाए sets की। Superiet हैं हर दिए ZHMC, It is the universal set.





(IV) Left Host open Intervol (a,b] @, Ja,b] = {NER: a<N < b} on the real line, we represent these intervals as shown below:

The length of each of the intervals

[a,b] is (b-a)

examples: (i) - 2013 = { NEIR: -2 < X < 34 (ii) (-2,3) $= \{n \in \mathbb{R}: -2 < n < 3\}$ (iii) [-2,3)={NFR: -25x <3} (iv) (-2,3]. = [neR:-2< x < 3].

* Power Set: The set of all subsets of a given set of A ; the bower set of A ; denoted by P(A). 3012 m (A) = m. dd m[p(A)] = 2m. Write au possible subsets of: Ami exist possible subsets of A E \$ 1, {43, ; p(A) = \(\dagger \); \(\frac{4}{3} \right\) 4ET, m(A)=1 . m P(A) = 2.7 = 21. Q. Write down all possible Jubsety
of A = {2,3}. This 9.272AT possible subsets of A \$\forall \text{2}, \{2\frac{1}{3}\frac{1}{

:.. P(A) = { \$ 5 \ 723 > \ 33 } {2,3} } 321(MV m(A)=2& $m \{ P(A) \} = 4 = 2^2$ write down all possible subsets As: 272A possible substets of A. 0, 5-13, 503, 513, 5-1,03, 50,13, 5-1,14 and 5-1,0,13. $(0,1) = \{ \phi, \{-1\}, \{0\}, \{1\}, \{-1,0\},$ {0,1}, {-1,1}, {-1,0,1}} で m [p(A)] = 8 = 23. Q. write down all possible subsets of 20: 21 of A do VIN at elements & 31/2 (2,34.

$$P(A) = \{\phi, \{1\}, \{2,3\}\}, \{2,3\}\}, \{3,\{3,\{2,3\}\}, \{3,\{2,3$$

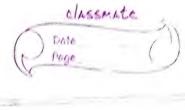
classmate (iii) c= [-8,0) = {x:x=R, -8 < x < 0} (iv.) D = (5,9] (x: x ∈ 1R, 5 < x ≤ 9} Operations on Sets Union of Sety: sets A 3482 The state of the s A={3,4,5,6} ex: 74,6,8,10} UB= 13,4,5,6,8,10)

ex: A={n:x is a prime muniter and B={x:x E·N, xisa.]. साम दे कि A={2,3,5,7} B= 1,2,3,4,6,12 : AUB= 1; 2; 3, 4, 5, 6; Till ex: A = [N:N is a positive integer]

and

B = [N:N is a negative integer] A= 11,2,3, ---

 $B = \{----3, -2, -1\}$ $AUB = \{----3, -2, -1, 1, 2, 3, ---\}$



Remark:

The union of myets A1, A2, A3, ...,

An is denoted by

(A1 U A2 UA3 U - ... U An)

= U A;

i=1

12.1 Intersection of Sets:

at set A 3912 B Graph, ANB 21

denote optit; at set & Graph

at 21721 elements & only alor

set A & B & Common &

Zelmu,

ANB = N: NEA and NEBY

: N € ANB ⇒ X € A OND X € B.

ex: A = { 1,3,5,7,9}

B = {23,5,7,11,13}

AOB={3,5,7}

ex: A=\n:xEN, nis a factor
of 12 and B= [N:NEN, nisa factor]
of 18 साप 2° Ab A= { (1), (3, (3), 4, (6), 123 B= { ((2) B), (6) 9, 18 5 = \ 1.2,3,63 ex: A={n: x=3n, ne Z} B=[x: x=cm, m {Z} सापा डे कि A= TN: NEZ and xissa mutible of 3 B={n:xEZ and x is a multiple of 4 .. ANB={x:xEZ and x is a multiple of both 384

= \n: n E Z and n is a multiple of 12's $=\{\lambda; \lambda=|2m,n\in\mathbb{Z}\}$ Hence, ANB = {x: x = 12m, n ∈ Z6 0. If A = (2,4) and B=[3,5)
, find AnB. $A = (2,4) = \{n: n \in \mathbb{R}, 2 < n < 4\}$ B=[3,5)=[N:NER,3<X<5] साप है कि ANB= {NineR, 3 < n < 49 [3,4] Benock: The intersection of m sets A1, A2, A3, ..., An is denoted by A1 n A2 n A3 n · · · · · · · Am) = n · A;

Diwigint Sety: - B B disjain

The sety A & B B ANB= 6.14

FORTH STATE ANB=6.14 If A = \(\begin{align*} 1,3,5,7,9\end{align*},

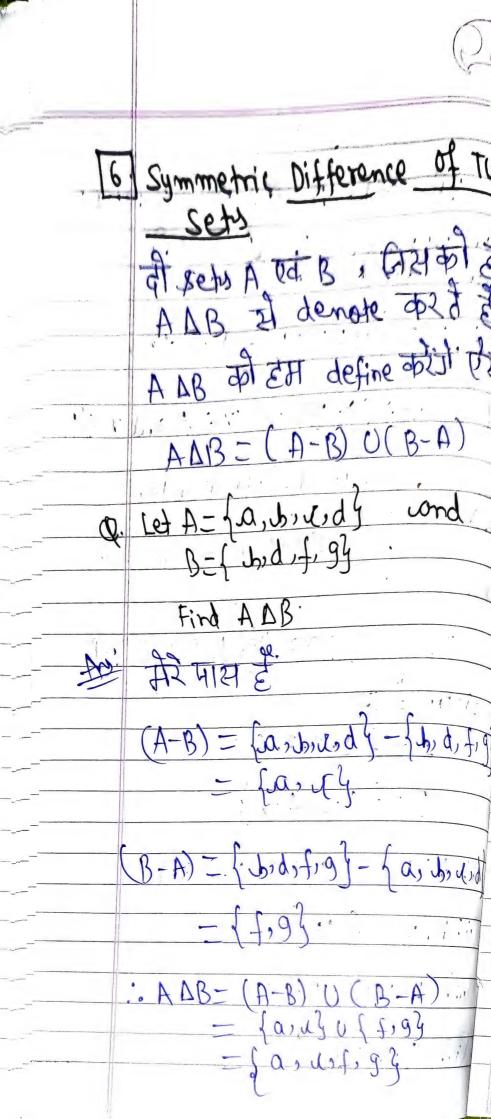
B = \(\begin{align*} 2,4,6,8\end{align*} \) and

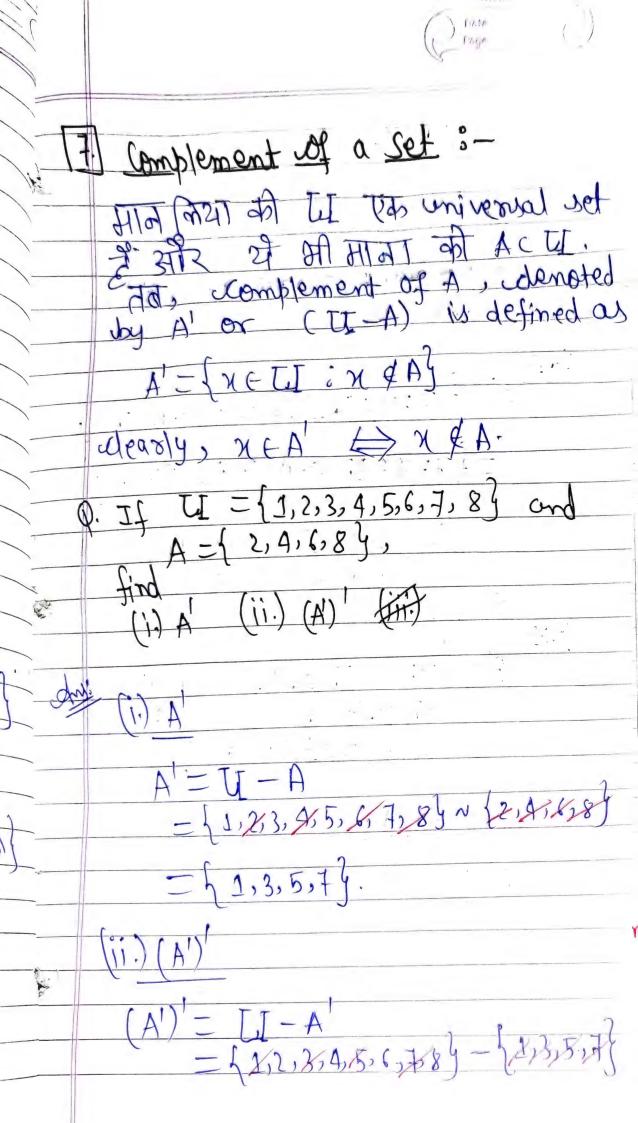
C = \(\begin{align*} 2,3,5,7,11\end{align*}

find (Ang) and (Anc)

what do you conclude. A={1,3,5,7,99 B= 12,4,6,8} $A = \{1, 3, 5, 7, 9\}$ $C = \{2, 3, 5, 7, 41\}$ Anc = (3,5,741...

5. Difference of Sety :-किसी भी sety A और B, जिसका difference (A-B) 2 321-691
define \$251. 121:2 (A-B)={n: neA and n&B} ZHAND XE(A-B) => XEA and X &B Q. If A= {x: x EN, x is a factor of 6] and B={XEN: X is a factor of 8} then find: (i) AUB (ii) AOB (iii) A-B (iv) B-A. किंग्न साम है कि A={1,2,13,63 B={1,2,4,8} (i) AUB = { 1,2,3,4,6,8'} (11) ANB = { 1;2}. Viii) A-B={(3,6) iv.) B-A={ 4,8}





= { 2,4,6,8}

Q let N be the universal set. (i) If A = {x: x ∈ N and x is odd},
find A'.

A'= { N: N EN and N is not al = [x: x EN and x is even?

(ii) If B= { n: NEN, nis divisible Find B' by 3 and 5

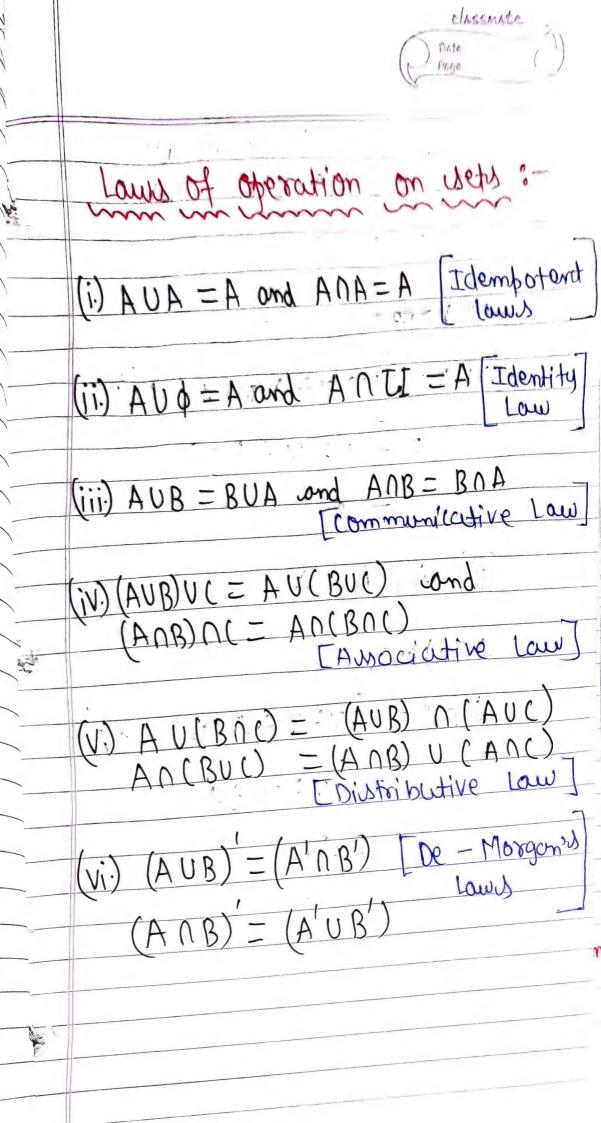
B'= N: NE N and Xis mot divisible by 3 or nist not divisible by 5.

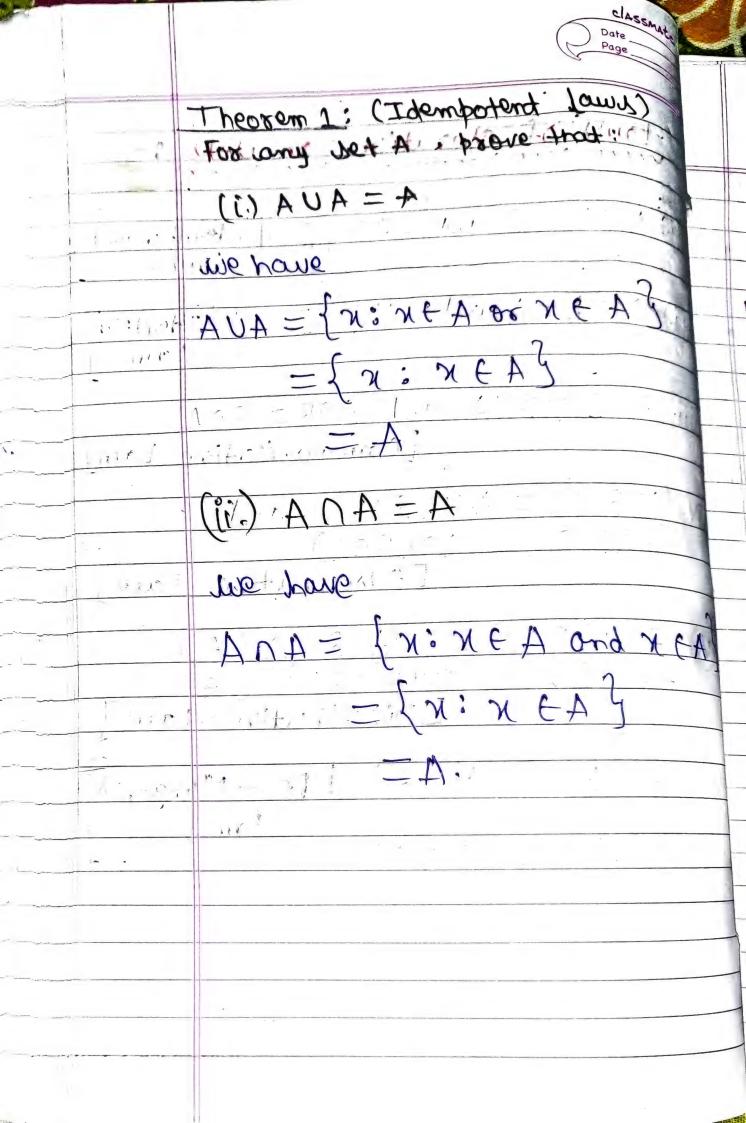
Some results on complementation:

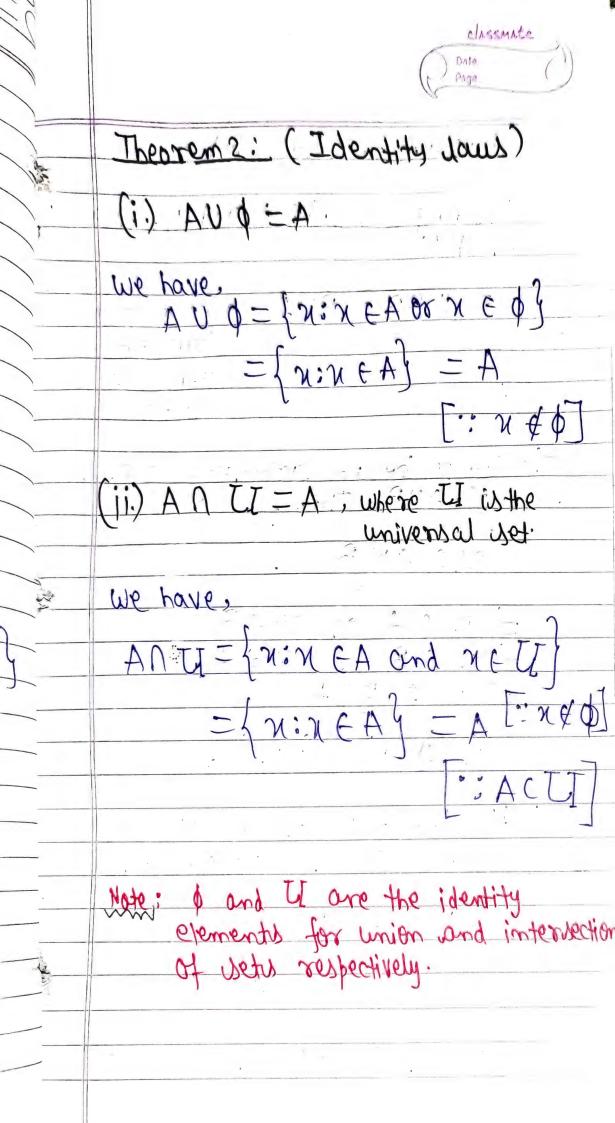
If A C U = \$

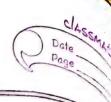
(iii) (A')' = A(iv) AUA' = UI (v.) Ana' = ϕ

(ii.) \$ = U









Theorem 3: (Commutative law)
For any two wets A and B, for that:

That:

Theorem 3: (Commutative law)

Theorem 3: (Commutative law)

Theorem 3: (Commutative law)

Theorem 3: (Commutative law)

Let x be an arbitrary elem

MEAUB.

=> MEA OR NEB => MEB OR NEA => MEBUA

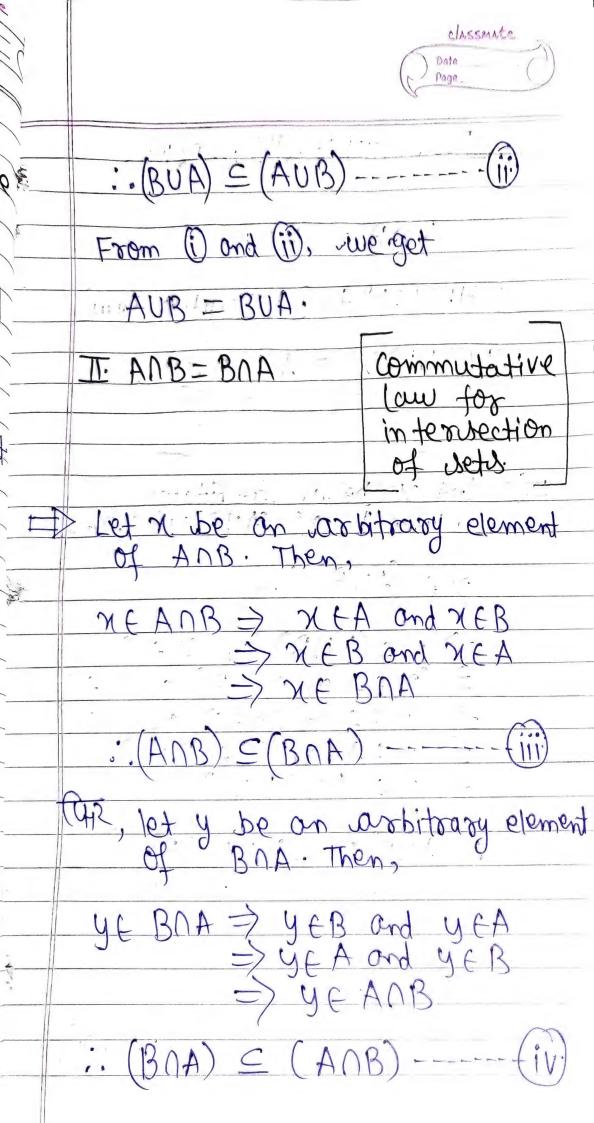
: (AUB) C(BUA)

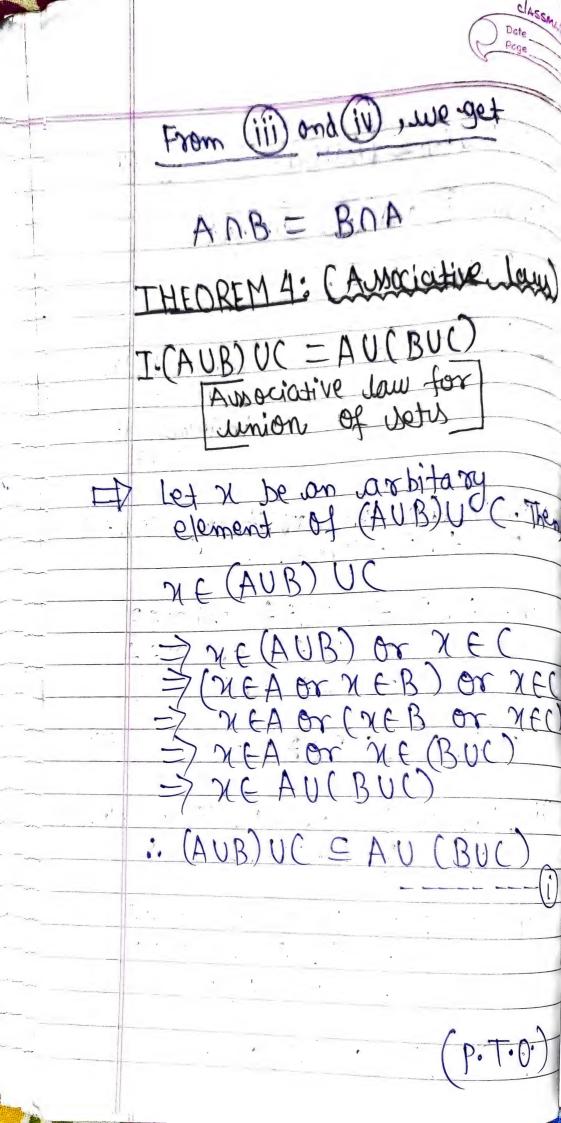
element of BUA. Then,

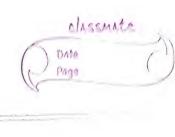
: 1 y E BU.A.

=> YEB ON YEA >> YEA ON YEB => YE(AUB) =

3)







1973,

Let y be on ar bitrary element of AU(BUC). Then,

YE AU(BUC)

THEN,

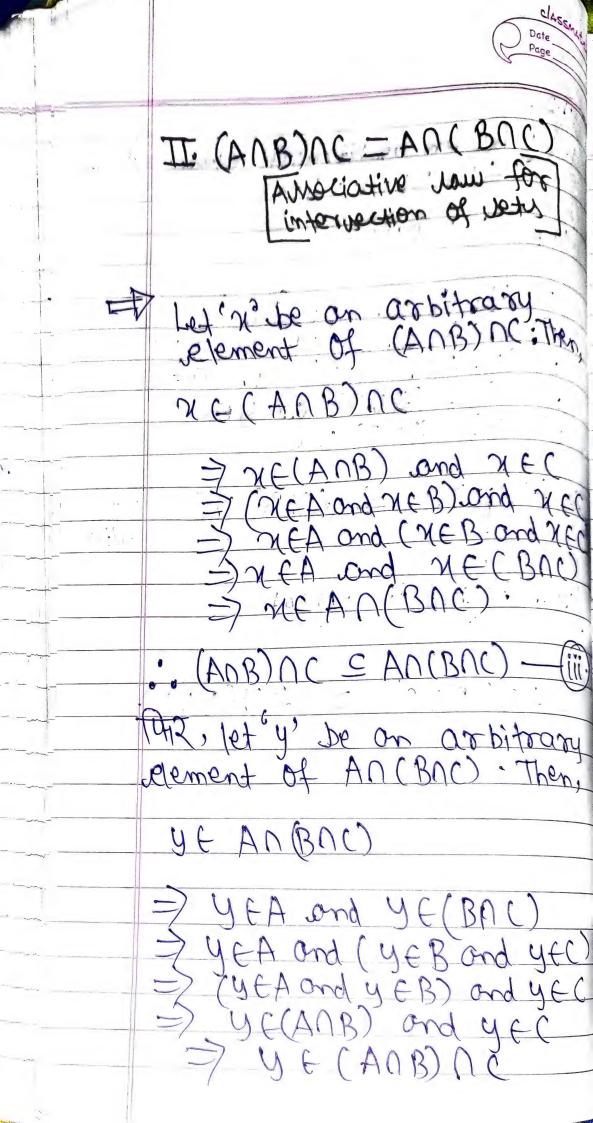
YEA ON YE (BUC)

⇒ y∈ A or y∈ (BUC) ⇒ y∈ A or (y∈ B or y∈ C) ⇒ (y∈ A or y∈ B) or y∈ C ⇒ y∈ (AUB) or y∈ C ⇒ y∈ (AUB) U C

: AUBUC) = (AUB) U

From (i) and (ii) we get

: AU(BUC) = AU(BUC)





: An(Bnc) = (AnB) n(- (iv) from (iii) and (iv), we get (ANB) nc = ANCBNC). Theorem 5: (Distributive Laus) For any three wets A, B, C prove that: (I.) AU(BOC) = (AUB) A(AUC) Distributive law of union over intensection.

let or be an arbitrary element of AU(BNC). Then, ME AU(BOC)

> x E A or X E (Bnc) > x E A or (X E B) and (X E C) > (X E A or X E B) and (X E A Or X E)

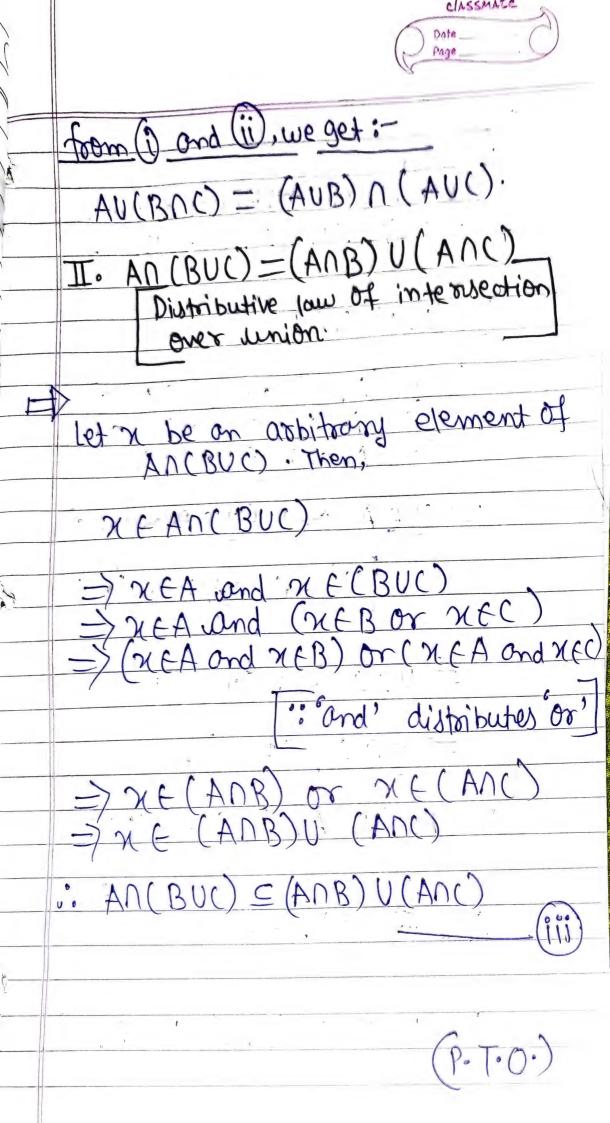
[" or distributes ond

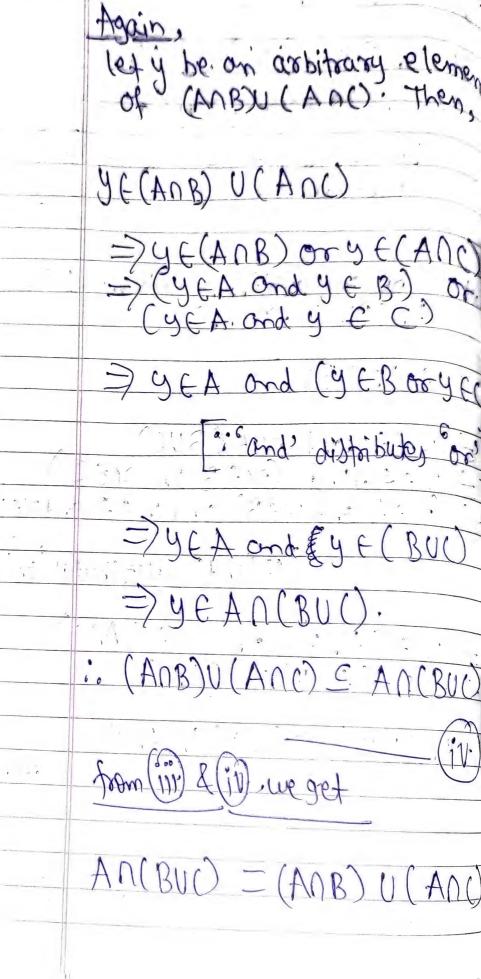
FXE(AUB) and XE(AUC)

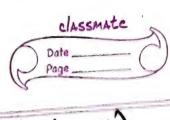


=> NE (AUB) n(AUC) : AU(Bnc) = (AUB) n(AUC) Again, let y be on arbitrary
element of (AUB) n(AUI)
Then, YE(AUB) n(AUC) =) yE(AUB) and yE (AUC) => (yEA or yEB) and (yEA or yEC) FA Or (YEB and YEC) "Or" distributes on => YEA or YE (BUC) DYE AU (BOC) :. (AUB) M(AUC) C AU(BM)

p.T.O.)







Theorem 6 (De-Morgan's Laws)

For any two weters A and B, prove

I. (AUB) = (A'NB')

The let x be un arbitrary element of (AUB)'. Then,

ME (AUB)

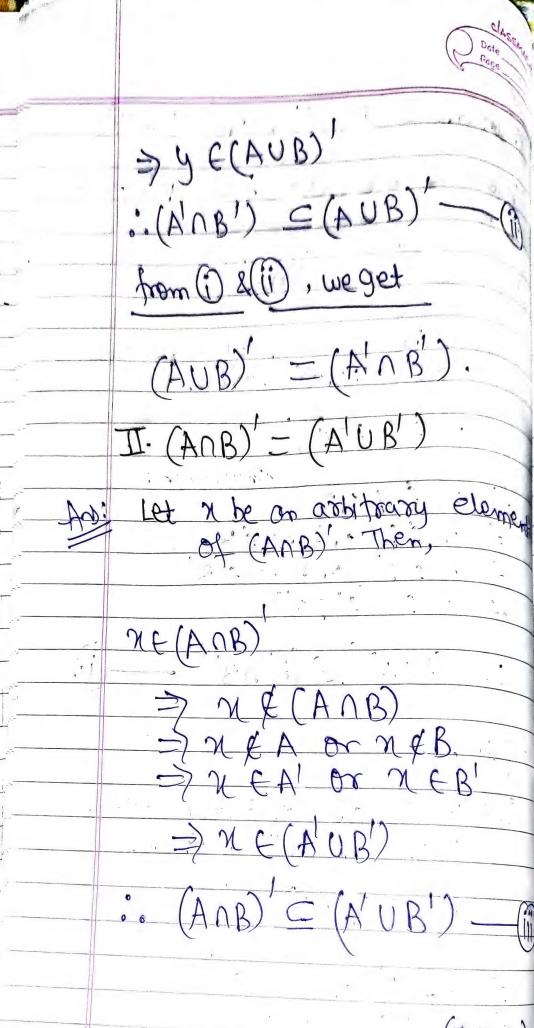
=> x & AUB => x & A ond x & B => x & A' and x & B' => x & (A' \(\Omega\)')

:. (AUB) = (A'nB')

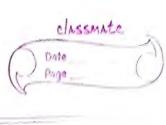
Let y be on arbitrary element

YE (A'NB')

⇒yEA' and yEB' ⇒y EA and yEB ⇒y E (AUB)

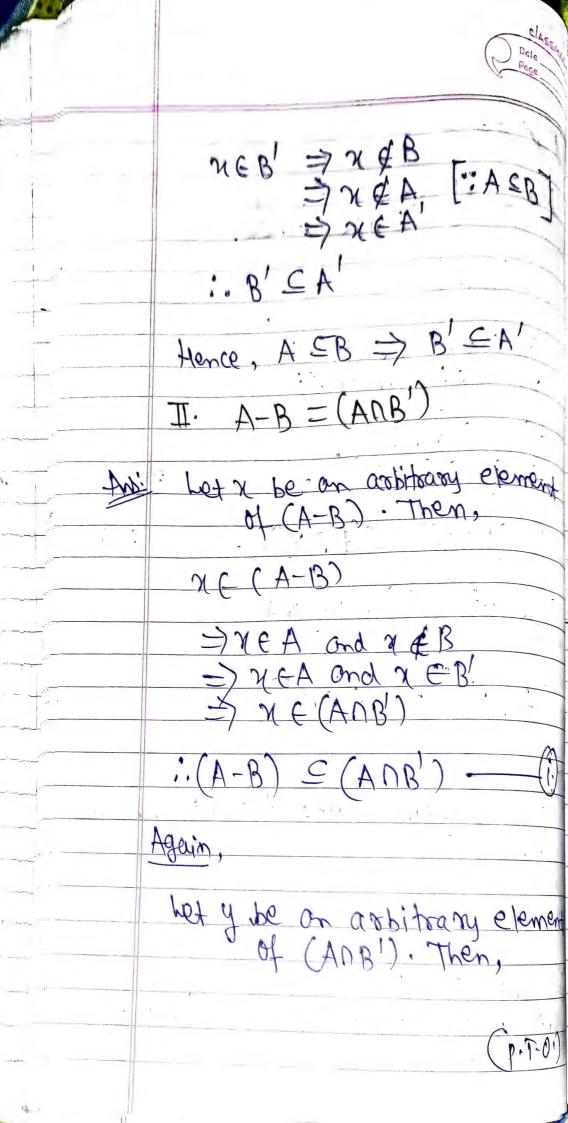


P. T. O.)



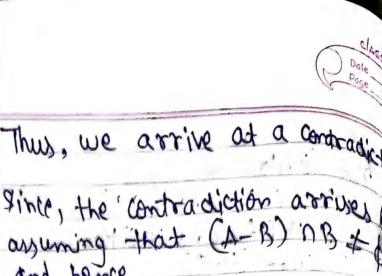
Again. let y be on arbitrary element ye (A'UB') JyEA or y €B => y & (ANB) :. (A'UB') = (ANB) from (iii) f(i), we get (ANB) = (AluB). Theorem 7: For vary two sets A and B, prove that: I. ASB > B'SA'

Let A = B be given & let x be an arbitrary element of B'. Then,



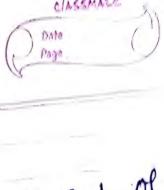
TYEA and NEB'

THE (A-B) ME (ANB) :. (AnB') = (A-B) Hence, from (1) and (ii) weget $(A-B) = (A \cap B')$ III. (A-B) (B = 0 If bousible, et (A-B) NB = p and =) XE(AB) and MEB (XEA and X&B) and XEB XEA and (X&B) and XEB) more x &B and NEB can never chold simultaneously.



(A-B) OB = O. TV. (A-B) U(B-A) = (AUB) - (ADB) Let x'be on arbitrary elemen of (A-B)U(B-A). Then, XE(A-B) U(B-A) =) re (A-B) or re(B-A) => (x ∈ A and x ∉B) or (x ∈ B and x ∉A) => (x E A or x EB) and (MEA orn &B) => ME (AUB) and ME (ANB) = (ANB)} .. (A-B) U(B-A) = {(AUB)-(ANB)

and hence



again.

let y'be an arbitrary element of (AUB) - (ADB) . Then,

ye (AUB) - (ADB). >y∈ (AUB) and y € (ADB)

=>(yeA or yeB) and (y & A or y & B)

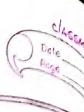
=>(yeA and y & B) or (yeB and y &A)

=> 4E(A-B) or y E(B-A) => y = (A-B) U (B-A).

from (iii) &(iv), we get.

(A-B) U (B-A) = (AUB)- (ANB).

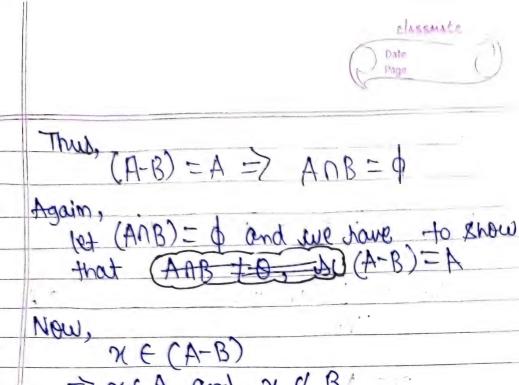
Po To Oa)



V. (A-B) = A ⇔ A ∩ B = 6 के कि जार के (A-B)=A. given & है निष्ठ ware के = 8 ता है। 31J12 possible et at: मान लिया कि नगड + 04 Hid Mat Ab YEARB. Then MEADS > MEA and MEB =) MC (A-13) and YEB A = (A-B) (given) =>(MEA and XEB) and NEB > XEA and (X & B Ond XEB) But, X&B and XEB both scan

Thus, we arrive at a contradiction.

Since the contradiction arises by arburning that ADB # \$ 1 40° A'NB = d.



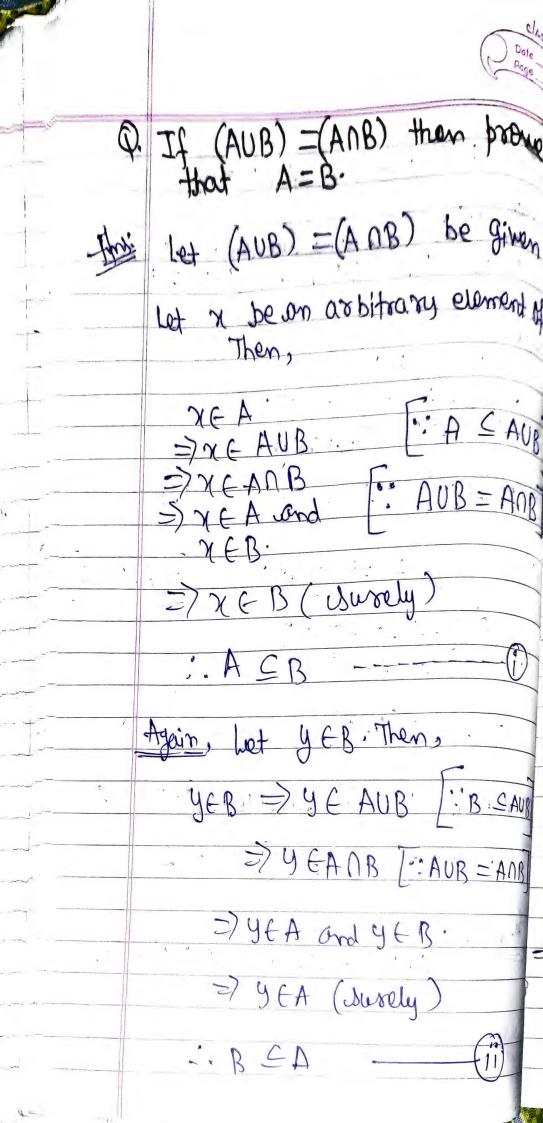
 $\Rightarrow x \in A \text{ and } x \notin B$ $\Rightarrow x \in A \text{ (surely)}$ $\therefore (A-B) \subseteq A \longrightarrow (V)$

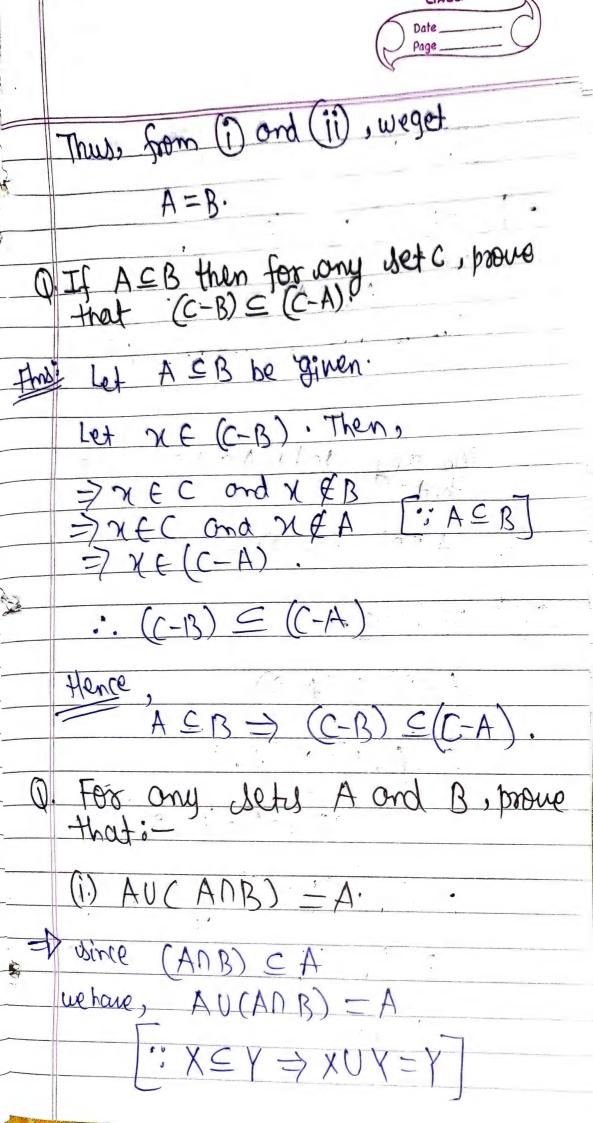
yeA => y ∉ B ⇒ y ∈ A and y ∉ B ⇒ y ∈ (A-B)

Thus from (V) & (Vi), we get (A-B) = A

$$ADB = \phi \Rightarrow (A-B) = A$$

Hence, $(A-B) = A \Leftrightarrow (A \cap B) = \emptyset$.







(ii.) An(AUB) = A

usince $A \subseteq (AUB)$,
us have $A \cap (AUB) = A$

: X C X > X N Y = X

For any Jets A and B, prone thed:

i) (A NB) U(A-B) = A.

we have,

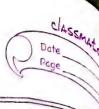
(AOB) U (A-B)

= (ANB) U (ANB)

"; A-B-(ANB)

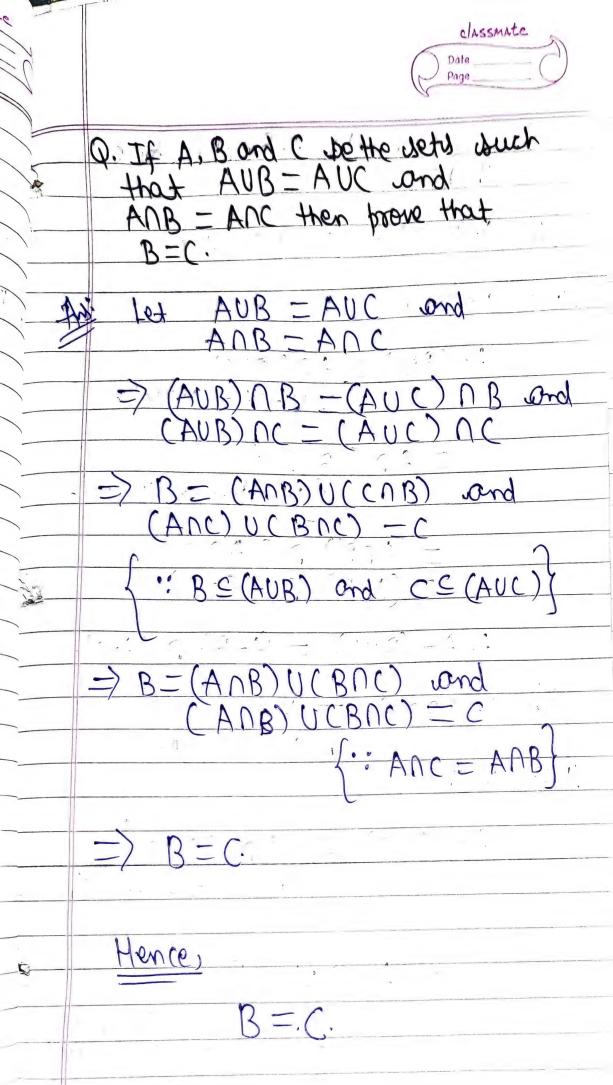
(BUB') - BUB'= U

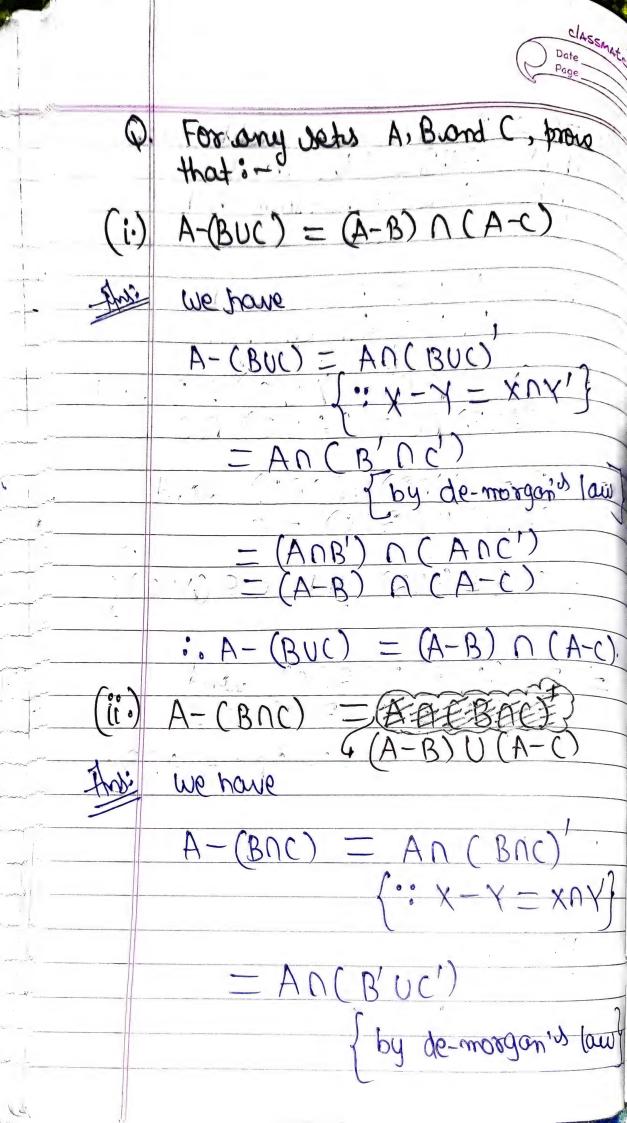
classmate (ANB) U (A-B) = A: (ii) AUCB-A) = (AUB) we have AU (B-A) : B-A = (BnA) AU (BOAT) = (AUB) n (AUA!) by distributive but AU(B-A) = (AUB). Q. If ANB' = & then prove that A=ANB and hence show that (potode)

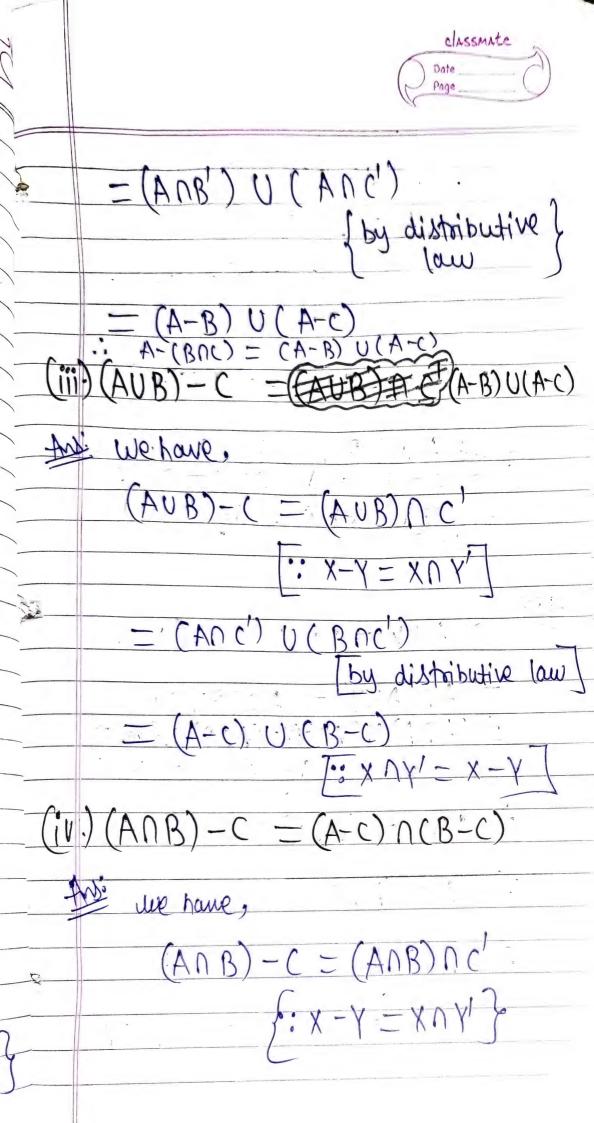


Let ANB = of be given. Then A=(AnII), where II is
the universal = AN(BUB') : BUB'= U = (AnB) U (AnB') (AnB) UD Further, A = AOB and let XEA. Then. MEA = MEANB => XEA and XEB => XEB (surely) .. A ⊆ B.

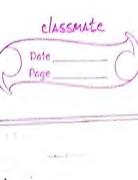
y w.



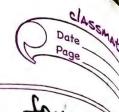




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\text{Construction} \\$$



Again, AUX = BUX $B \cap (A \cup X) = B \cap (B \cup X)$ $(B \cap A) \cup (B \cap X) = (B \cap B) \cup (B \cap X)$ by distributive law?



Q show that the following four conditions are equivalent:

(i) A CB
(ii) A-B =
$$\phi$$

(iii) AUB = B
(iV) ADB = A

 $N_{\Theta W}$, $(i) \Rightarrow (ii)$

In order to prove the required result, we will show that:

$$(i) \Leftarrow (ii) \Leftrightarrow (ii) \Leftrightarrow (ij) \Leftrightarrow (ij)$$

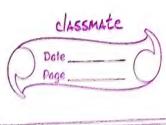
Let A CB be given

Then, there is no element of A which is not in B.

: there is no element of A which is not in B.

Hence,

 $A CB \Rightarrow A-B = \emptyset$ and therefore (i) \Rightarrow (ii.)



 $: (iii) \Leftarrow (ii)$

Let A-B= of be given. Then,

A-B-\$ \Rightarrow element of A

is in B:

A-B-B \Rightarrow element of A

A-B-B \Rightarrow A-B

AUB = B.

Thuy, A-B= 0 -> AUB= B and

 $(ni) \Rightarrow (iv)$:

Let AUB = B be given; Then,

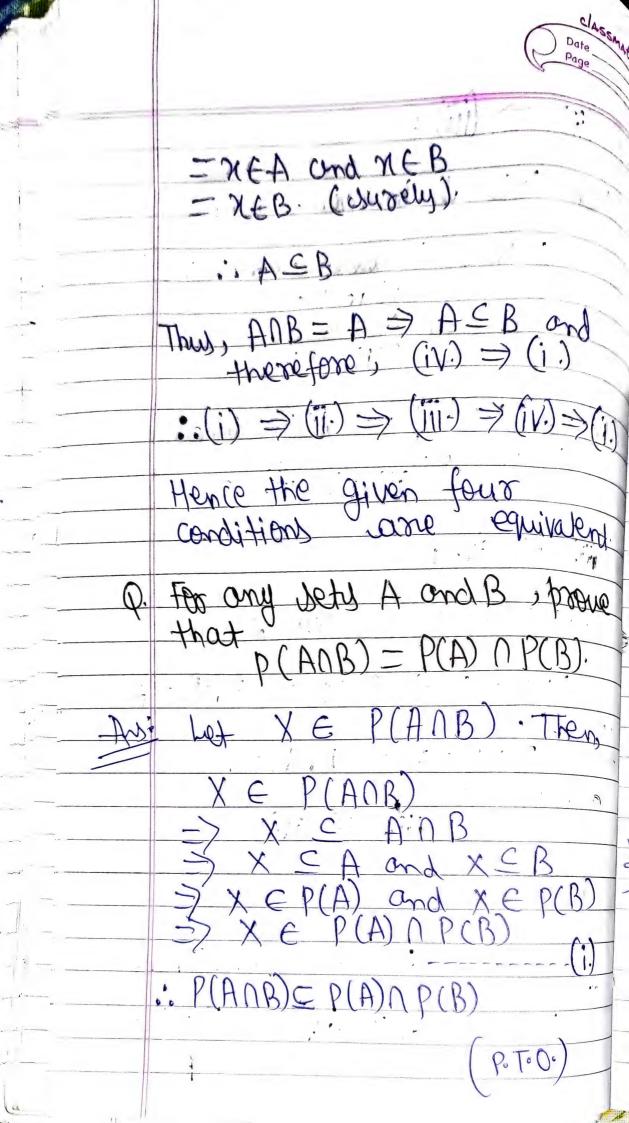
AUB=B => ACB => ANB=A Thus, AUB=B > ANB=A

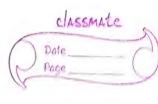
and therefore;

 $(iv) \Rightarrow (i)$

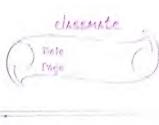
Let (ANB) = A be given. Then,

NEA = NE ANB LIA = ANB





Again, let YE P(A) n P(B). Then, YEP(A) NP(B) > YEP(A) and YEP(B). > YCA and YCB > YCA and YCB > YCA ANB. · P(A) n P(B) n P(AAB). — (i.) from (i) 4(ii), we get $P(A \cap B) = P(A) \cap P(B)$. Q For any two Jets A and B, prome that 3 P(A) UP(B) = P(AUB) But, P(AUB) is mot mecessarily a subset of P(A) UP(B). element of P(A) U P(B). Then, $\chi \in P(A) \cup P(B)$ \Rightarrow $X \in P(A)$ or $X \in P(B)$ \Rightarrow $X \subset A$ or $X \subset B$.

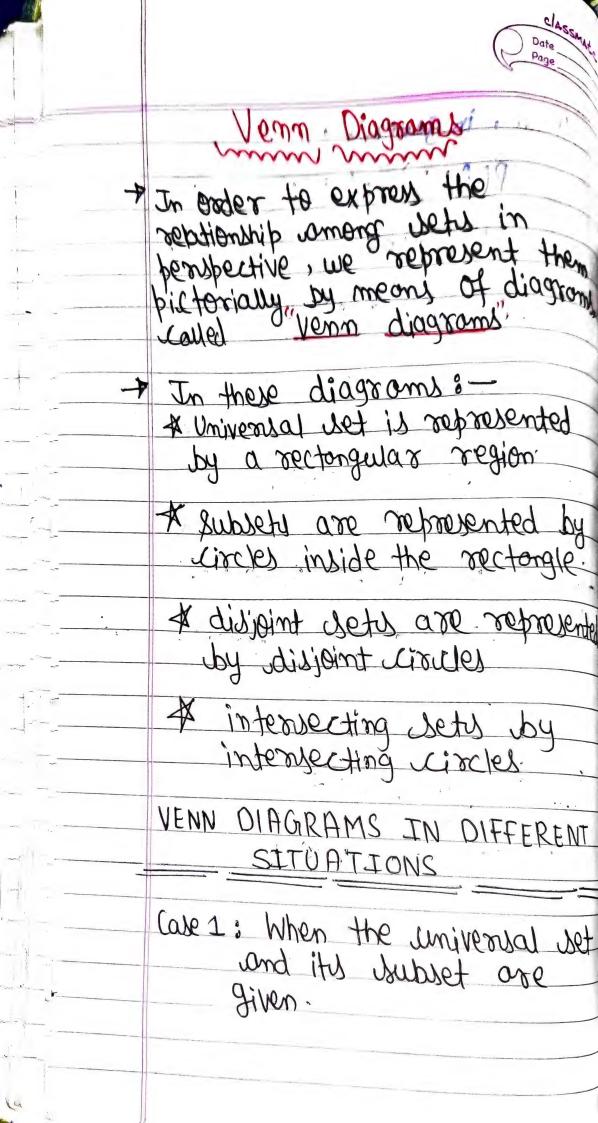


Hence, in general, $P(AUB) \neq P(A) \cup P(B)$ Q. If P(A) = P(B), prove that A=B. let P(A) = P(B). Then, ACA = A.EP(A) [: P(A) = P(B) =) A < P(B) =) A < B --- (T) again, BCB => B EP(B) => B E P(A) [::p(B) = P(A)] 7 BSAI-

from (i) e(ii), neget

A SB and B SA

Hence A=B.



HIN MUIT AS II revivend set 24 let A = U. EH la virile draw to la rectongle to Fig.

The rectongular region & de U

represent to Fill of the A tot

circular region & de A tot

represent to Fill & De A tot

represent to Fil CX: Let TT = [1,2;3,4,5,6,7] 4 A=[1,3,5,7] अब हम उपर दिए गए तरीके थे Venn diagram dolly 34/2 $A' = \{2, 4, 6\}.$

Leve harming I (ale 2: When two intersecting musical of II was give at intersecting bubblets A

B of U apt represent

absorb fact circle and

intersecting a circle and

rectangle of Fig. Zal circles del common region (A-B) whow H A of region Eligical E (B-A) whow of? U



S CX

Let II = {1,2,3,4,5,6,7,8} be the universal set, and let

A= (113, 4), 5 } 4 1B= (2,4,5,6)

det > - ANB = { 4,5}

We draw the Venn diagram, as whown in the given figure

Mearly,

 $(A-B) = \{1,3\}$ $\{$

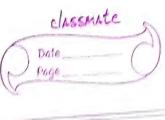
 $(B-A) = \{2,6\}$

Case 3: When two disjoint be given. A 31R B of disjoint subject Ups universal sets I do represent do to the Editory
It disjoint circles adjust
The rectongle of sizz let [= 1,2,3,4,5,6,7 be the universal set, and let A= [1,3,5] & B={2,4} be two of its disjoint subs clearly, ANB= 0

ZAMU EH offet fill de Tre Tolas 21
Venn diagram dott VIII 0 ckarly, AOB - 0, (A-B) = {1,3,5}=A and $(B-A) = \{2,4\} = B$ A' - \2, 4,6,7\ $B' = \{1,3,5,6,7\}.$ (a)e 4: When BCA ETL. In this case, we draw two concentric Circles within a rectorgular region. The immer circle represents B and the outer windle represents A.

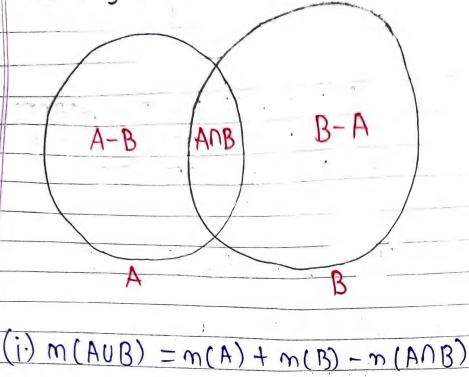
let [= [3,2,3,4,5,6,7,8] be the universal set, and the universal set, and $A = \{1,3,5,7\}$ be its subsety. $B = \{3,7\}$ be its subsety. U Then, clearly BCA. 37d EH veno diag som dell vit ANB= B= {3,7} AUB = A = (1,3,5,7 g. (A-B) - { 1,5} (B-A) = b& A = {2,1A,6,84 $B' = \{1, 5, 2, 4, 6, 8\}$

1



Some results derived from very Diagrams

For any sets ABIC, we have:



(ii) If ANB =
$$\phi$$
, then $m(A)$ m (AUB) = $m(A)$ + $m(B)$ - $m(A)$ + $m(B)$

(iii) m(A-B) + m(ADB) = m(A)

(iv) m(B-A) + m(ANB) = m(B)

 $\left\{ m(A) + m(B) + m(C) + m(A \cap B \cap C) \right\}$ $- \left\{ m(A \cap B + m(B \cap C) + m(A \cap C) \right\}$



Q. If A and B are two webs buy that n(A) = 27; m(B) = 35 and m(AUB) = 50, find m(ADB).

 f_{mi} m(AUB) = m(A) + m(B) - m(AOB) $\Rightarrow 50 = 27 + 35 - m(AOB)$ $\Rightarrow m(AOB) = 62 - 50$ $\Rightarrow m(AOB) = 12$

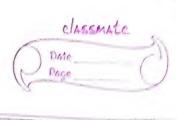
Hence, m (ANB) = 12.

If A and B are two vets containing 3 and 6 elements respectively, what can be the maximum no of elements in AUB? Find also the minimum no of elements in AUB?

" m(AUB) - m(A)+m(B)-m(ANB)

caseI

from (i), it is aleas that m(AUB) will be maximum when m(ADB)=0



In that case,

m(AUB) = m(A) + m(B)

= 3+6 =9

: maximum number of elements in (AUB) = q.

Case II

from (i), it is clear that m (AUB) will be minimum when in (ANB) is

maximum i.e., when m (ANB)-3.

In this case,

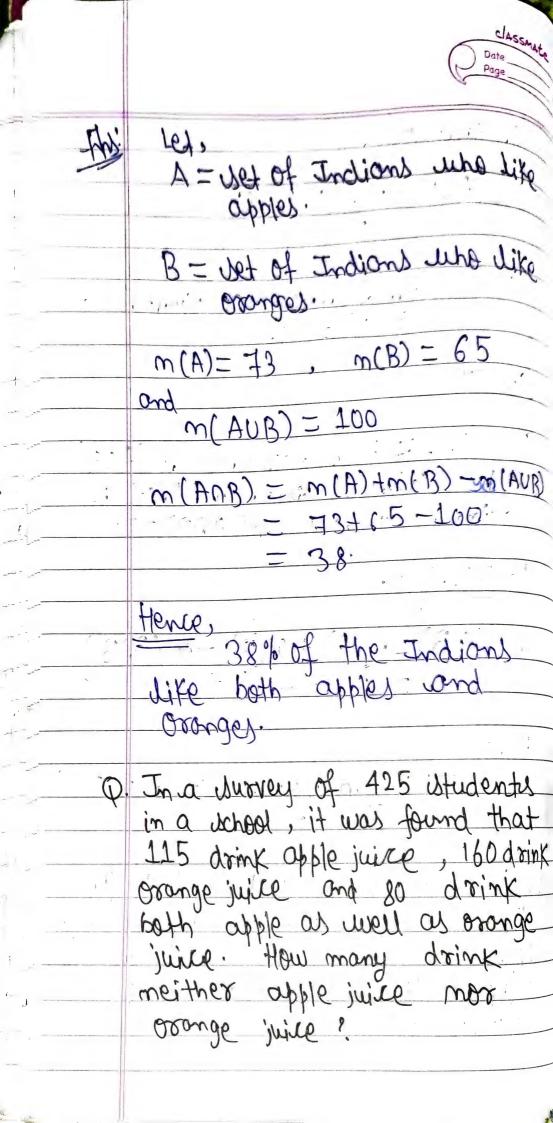
m(AUB) = m(A) + m(B) - m(ADB)= (3+6-3) = 6

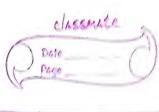
Hence

Minimum no of elements = 6. in (AUB).

Q. A survey shows that 73% of the Indians like apples, whereas 65%. Like oranges what percentage of

Indians like both apples and oranges





II = whet of all students warreyed,

A = whet of all students und

drink apple juice.

B = whet of all students und

drink orange juice.

Then,

m(U) = 425 m(AnB) = 80 m(A) = 115m(B) = 160

: m(AUB) = m(A) + m(B) - m(ANB)

= 115 + 160 - 80

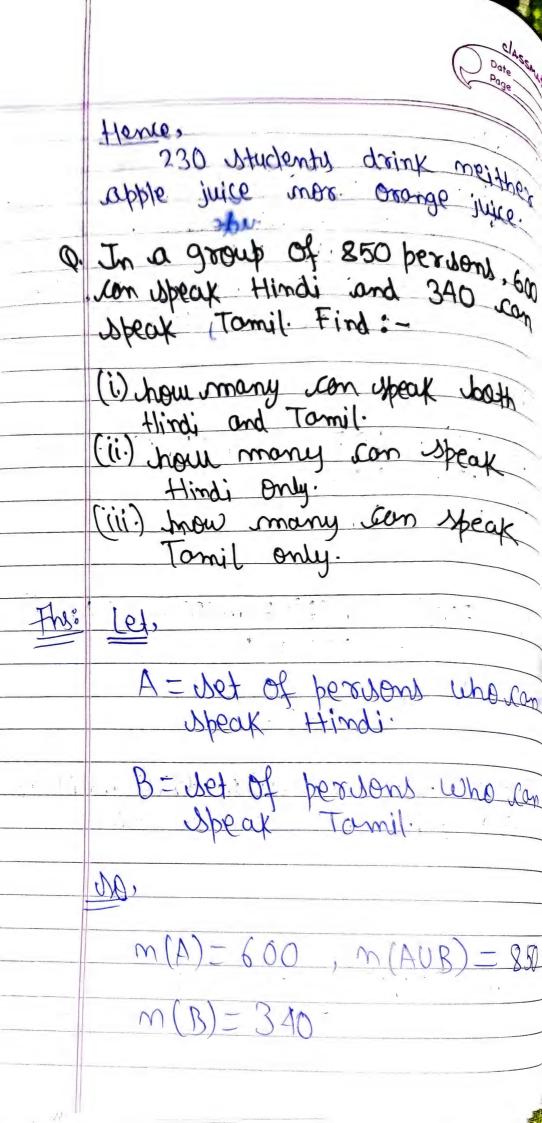
= 27 5 - 80

= 195.

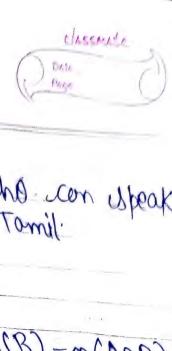
Set of studenty who drink meither apple juice mor orange juice

 $= (A' \cap B')$ = $(A \cup B)'$ $= m(\Psi) - m(A \cup B)$ = $A \cup B$ = $A \cup B$ = $A \cup B$ = $A \cup B$

= 230.



1.



1) yet of persons who can speak both Hindi and Tamil.

= (AnB)

m(AUB) = n(A) + n(B) - n(AnB) = (600 + 340 - 850) = 90

Thus, 90 persons can speak both Hirdi and Tomil.

(ii) Set of fersons who speak Hirdi

A-R D D

Titib

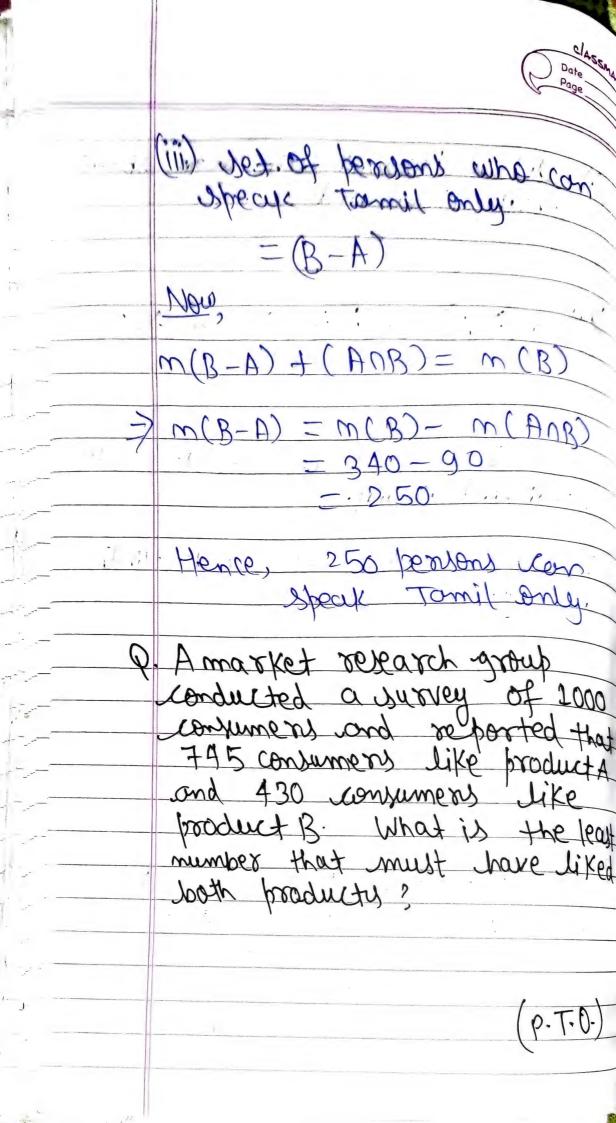
 $\frac{N\omega}{m(A-B)+m(ANB)}=m(A)$

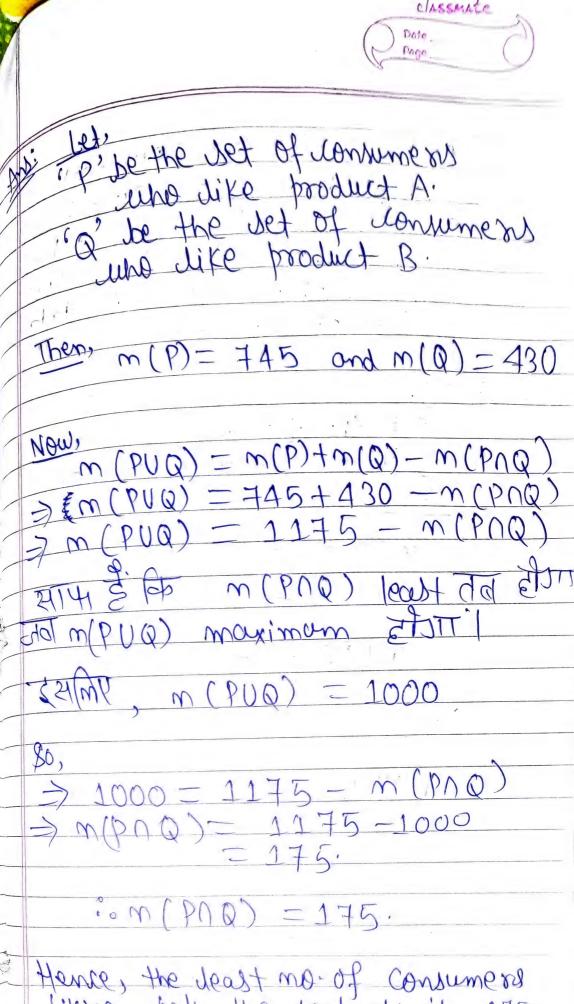
 $\Rightarrow n(A-B) = m(A) - m(AnB)$ = (600 - 90)

Thus, 510 persons can speak Hindi

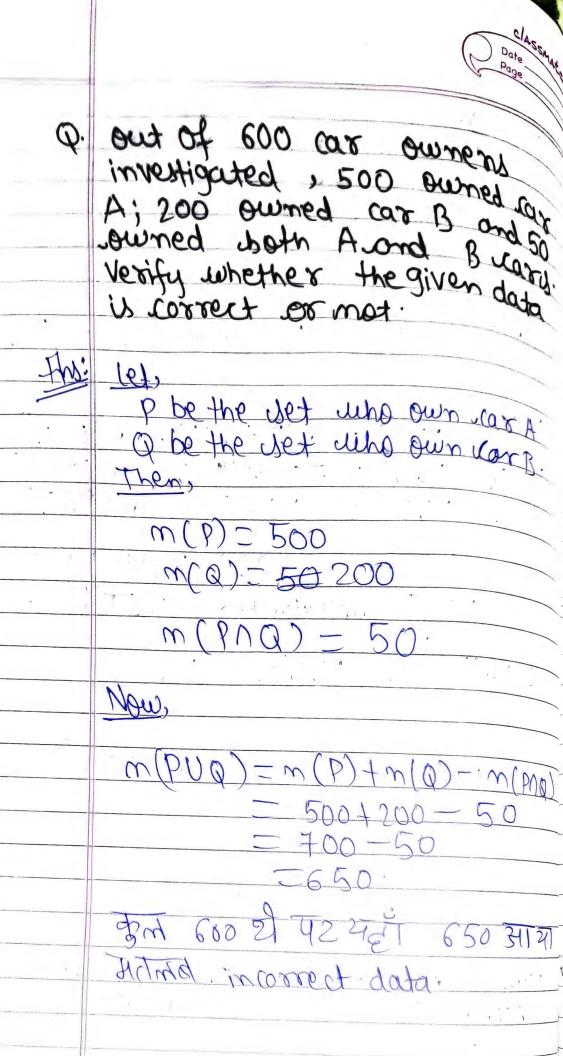
2

only.





Hence, the deast mo-of consumers liking both the products is 175



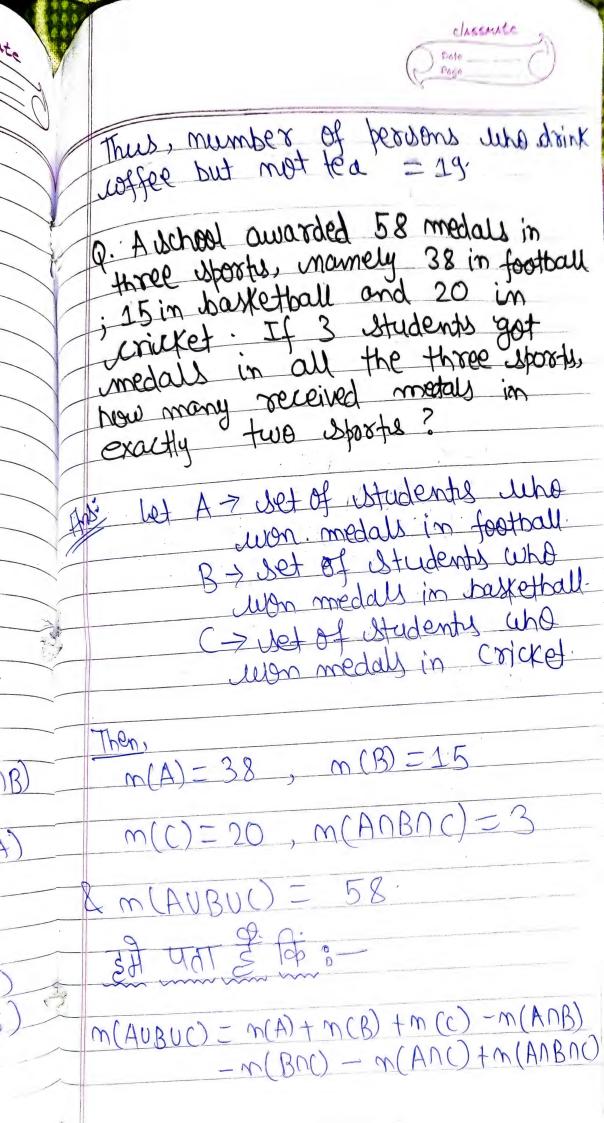


Ina group of 52 persons, 16 drink tea but mot coffee and 33 drink tea. Find 3— (i) how many drink tea and loffee (ii) how many doing coffe but मान लिया कि A= set of pensons who drink tea. B= set of pensons who drink coffee.

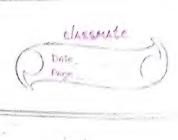
(A-B)= set of pensons who drink tea but not coffee.

B-A) = set of pensons uno drink coffee abut mot tea.

	Date Page
	22.0
	दिया इआ है कि :-
	m(AUB) = 52 m(A-B) = 16 m(A) = 33
	set of pensons sund drinktea and coffee soth.
1	=(ANB)
	Mgw, $m(A-B)+m(A\cap B)=m(A)$ $= m(A\cap B) = m(A) - m(A-B)$ $= m(A\cap B) = m(A) - m(A-B)$
	= 17.
	Pensons who doink coffee but
	m(AUB) = m(A) + m(B) - m(ADB)
	= 52+17-33
	1800) = 36
J	$m(B-A)+m(A \cap B) = m(B)$ $\Rightarrow m(B-A) = m(B) - m(A \cap B)$ = 36 - 17
	<u>- 19.</u>



m(ANB) + m (BNC) + m (ANC) = m(A) + m(B) + m(C) + m(AnBac) - m (AUBUC) $= \{(38+15+20+3)-58\}$ = 76-58 = 18. Q In a committee, 50 people In a commutation of these two longuages? मिष्ठः दिया हुआ इ People who speak Hindi = 50 People who Speak English = 20 People who speak both English and Hindi To find: people who speak at least one of these two longuages.

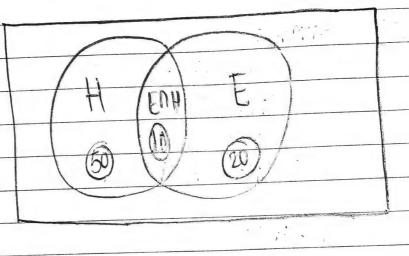


let us consider,

People who speak Hindi = n(H) = 50
People who speak English = n(E) = 20
People who speak both English and
Hindi

People who speak atleast one of the

two longuages = m (HUE)



Now, we snow that,

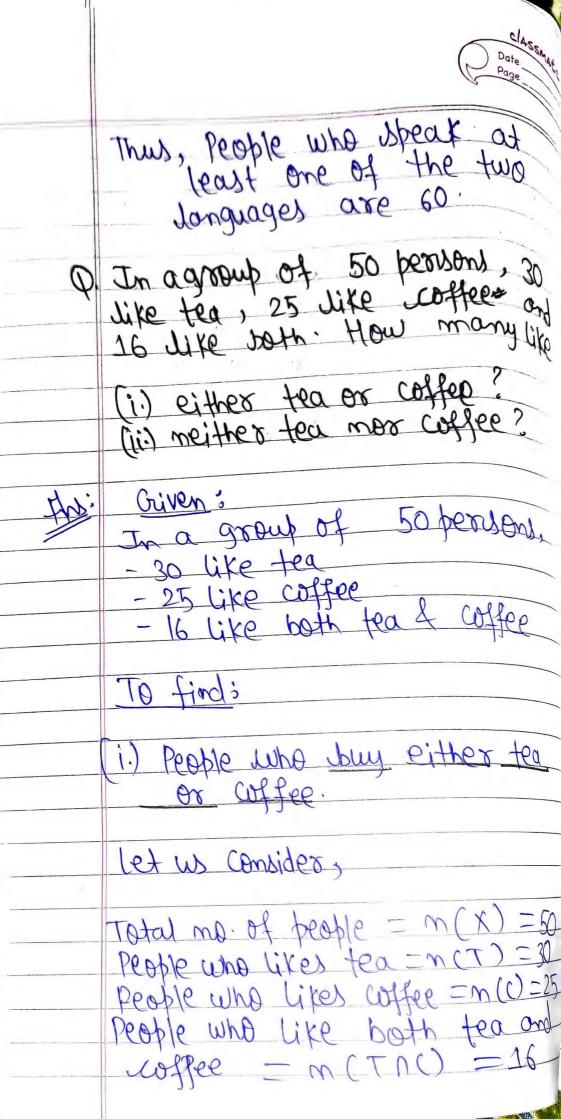
m(AUB) = m(A) + m(B) - m(AOB)

tracks fall.

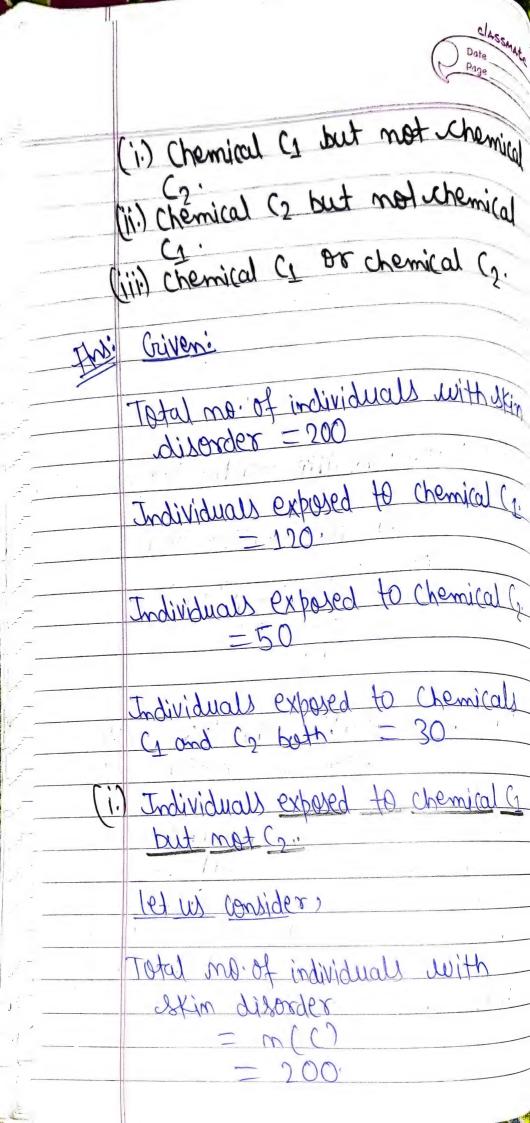
m(HUE)=m(H)+m(E)-m(HAE)

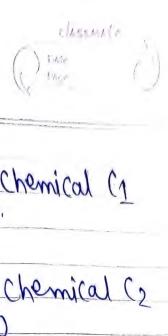
= 50+20.70

= 60,



people who like either tea or coffee =m(TUC) m(TUC) = m(T) + m(C) - m(TnC)=30+25-16= 55 - 16= 39... 11.) Peoble who like neither tea now coffee people who like neither tea mor Loffee = m(x) - n(Tuc)= 50 - 39 N. = 11 Therefore, people who like neither tea nor coffee = 11. Q. There are 200 individuals with a Skin disorder, 120 had been exposed to the chemical Cy, 50 to Chemical C2, and 30 to both the chemicals Cz and Cz. Find the mo. of individual exposed to:-(Poto O.)





Individuals exposed to chemical (1

Individuals exposed to chemical (2 $=m(c_2)=50$ Individuals exposed to chemical Gard

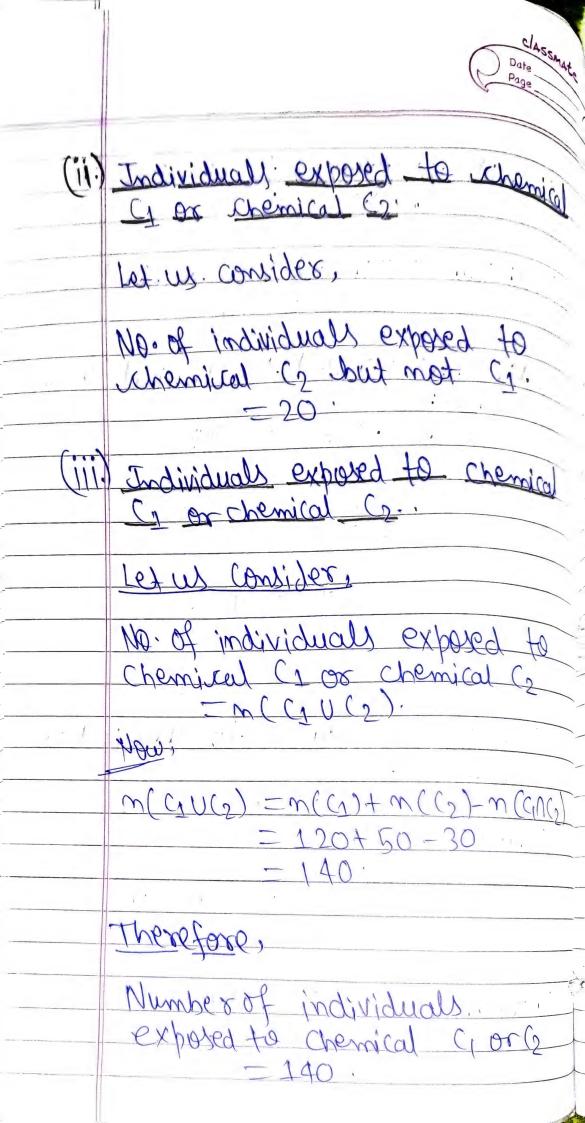
C2 both - m((1)(2) = 30 N=500

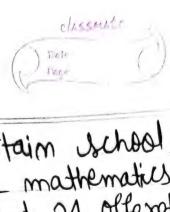
50/

Individuals exposed to chemical Cz but not (2 = m (C1-C2)

Now, $m(C_1-C_2)=m(C_1)-m(C_1)(C_2)$

= 120 - 30 therefore, mo of individuals exposed to shemical a but not C2





Q. In a class of a certain school, 50 students, offered mathematics, 42 offered biology and 24 offered both the subjects. Find the mo. of students offering:

(ii) biology only
(iii) any of the two clubjects.

Mi Oriven:

Number of Utudents Offered Maths. = 50 Number of Hudents Offered Biology = 42 No. of Students Offered bot Mathematics

i) No. of students of ferred Maths only

Let us Consider

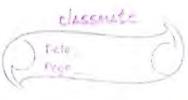
No. of Students Offered Maths = n(M)=50 No. of Students Offered Biology: n(B)=42

No of Students offered Maths &
Biology both = m(MDB) = 24.

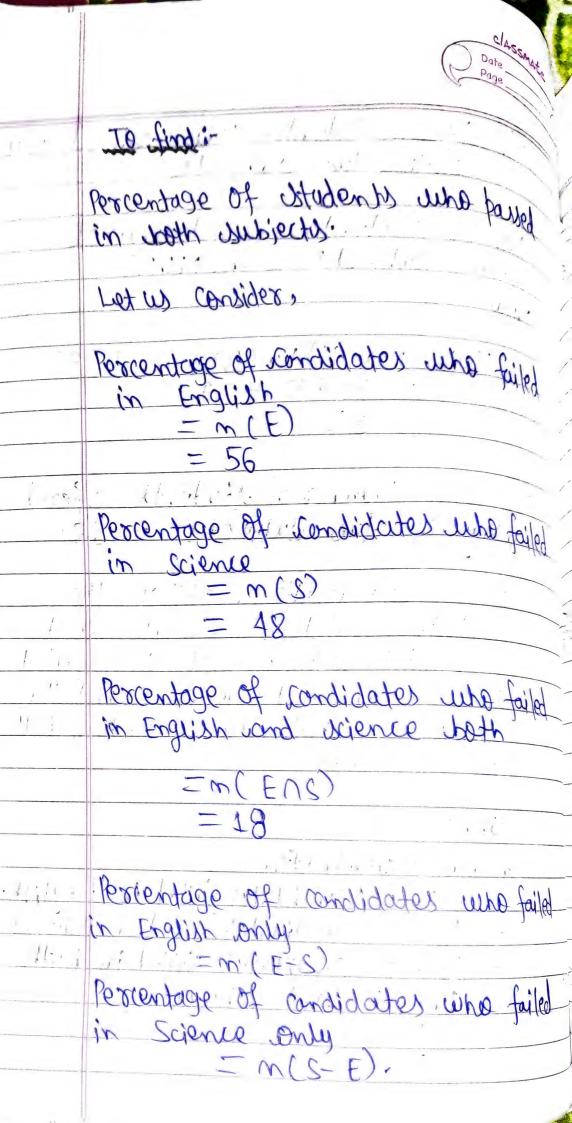
No. of students offered Mathematics only = m (M-B)

(0, -, 0.

U 50 Now m(M-B) = m(M) - m(MDB) = 50 - 24 No. of Students offered Biology Only. No. of students offered Biology Now, 1 m(B-M)=m(B)-m(MOB) 42-20 Therefore, No. of students offered Biology Only

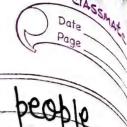


(111) No. of students whom offered any No. of students offered any of two subjects = m (MUB) NOW, w(MNB) = w(W)+w(B)-w(WUB) = 50+42-24. - 140 Therefore, Number of Students Offered any of two subjects = 68. Q. In an examination, 56% of the randidates failed in English and 48% failed in science. If 18% failed in both English and science, find the the subjects. And: Criven & noitanimaxs no nt - 56% of cardidates failed in English. - 48% of condidates failed in science.
- 18% of condidates failed in both English and ocience.



W. W.

checonte Now, = m(E) - m(ENS)= 156 + 18 = 38. m(S-E) = m(S) - m(SnE)=: A8 - 18 = 30 There fore, Percentage of total condidates who failed = m(E-S) + m(S-E) + m(ENS)= 38 + 30 + 18 ... = 860/0 Henre, The percentage of condidates who bassed in South English & Science = 14%.



Q. In a group of 65 people

40 like cricket and tennis.

both cricket and tennis and

How many like tennis and

How many like tennis and

ent cricket? How many life

tennis?

Ansi Given;

In a group of 65 people

- 40 people like both cricket

- 10 people like both cricket

and termis.

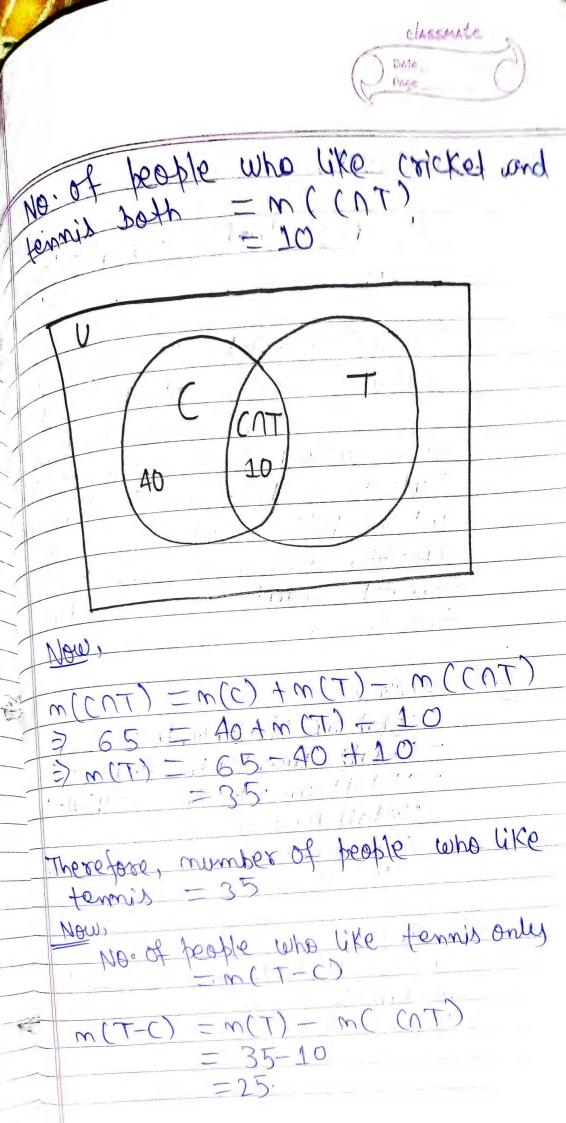
To find:
- Number of people like tenny
- Number of people like tenny

No. of people who like cricket = m(c) = 40

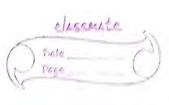
Let us consider,

No. of people who like tennis

No. of people who like cricketor tenns = m(CUT) = 65



Therefore, the mo of people who like terming only: Q A school awarded 42 medals in hockey, 18 in basketball and 23 in cricket, if these medals were bagged by a total of 65 Studenty and only 4 studenty got medall in all the three sports, how many students recieved medals in exactly two of the three sports? Givens - Total mo of whidenly = 65 - Medals awarded in Hockey = 12 - Medals awarded in Basketball=18 - Medall awarded in Cricket = 23 - 4 Students got medals in all the three sports. To find: No. of students who received medals in exactly two of the three sports. (P. T.O.)



Total number of medals - Medals awarded in Hockey + Medals awarded in Baskethall + Medals awarded in Cricket Total number of medals =42+28+23=83.It is given that 4 istudents got medall in all the three sports. Therefore, the mo of medals received by those 4 students: = 4 x 3 = 12 the no of medals received by the rest

the ma. of medals received by the rest
of 61 students.
= 83-12 = 71.

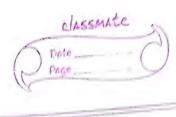
Among these 61 students, everyone at least received 1 modal.

The refore, the mo. of extra medals

= 71-1x61 = 10

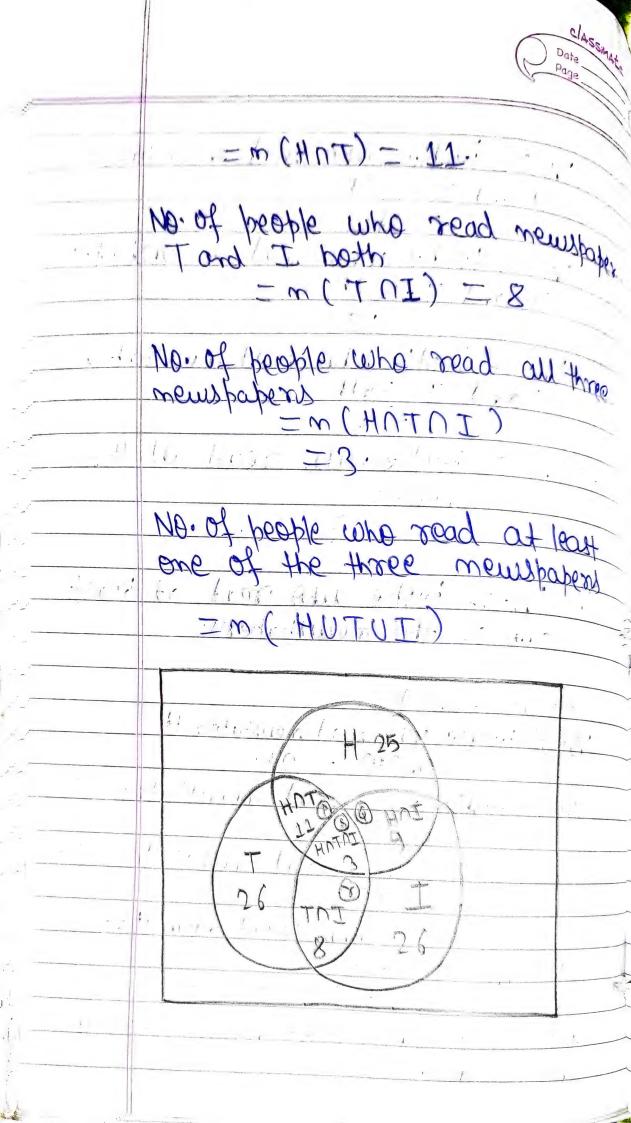
The refore, we can say that 10 studenty
received more than one and less than
three medals, or we can say that

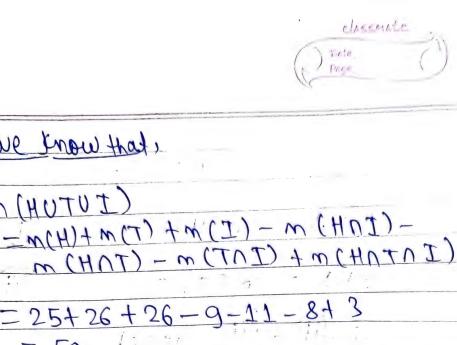
10 students received medals in exactly two of three sports. Q. In a survey of 60 beable, it was found that 25 beable read membaber H, 26 read nembers of membaber to see the second membaber to second membaber to see the second membaber to second me T, 26 read newspaper I, g read both H and I, 11 read both H and T; 8 read both Tond I, and 3 read all the three newspapers. Find: (i) The mumber of people who read at least one of the (ii.) The number of people who read exactly one newbater Si Given: - Total mai of people = 60 - Mos of people who read - Mos of people who read - No of people who read nembraper I = 26 P.T. 0.



- No. of people who read newspaper Hand I both - No. of beoble who read members -. No. of people who read meuspaper Tond I both -> No. of people who read all three newspapers = 3 (i) No. of people up read at least one of the neuthabers. Let us consider, = m(H) = 5. No. of people who read newspaper T =m(T) = 26. NO. of people who read newspaper I. No. of people who read newspaper H and I both = 9. No of people who read newspaper H

and I both





m (HUTUI)

we know that,

= 25+26+26-9-11-8+3

Therefore, Humber of teople who read at least one of the three newspapers

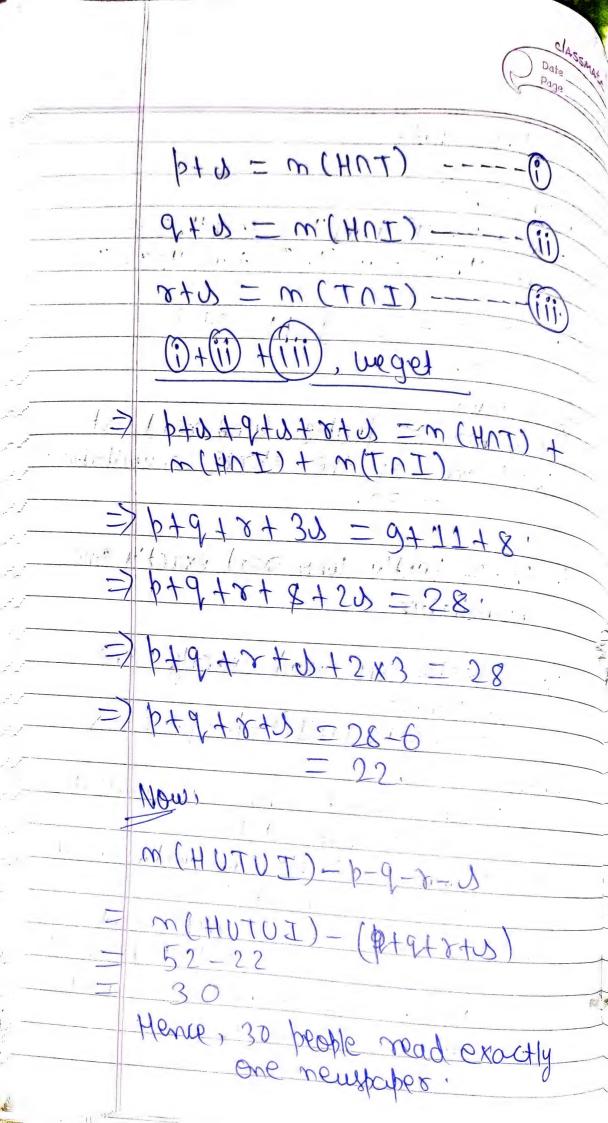
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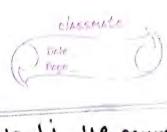
No. of people who read exactly one

meinsperber = m(HUTUI) - p-q-r-swhere, b- Number of people who read newspaper Hand T but not I.

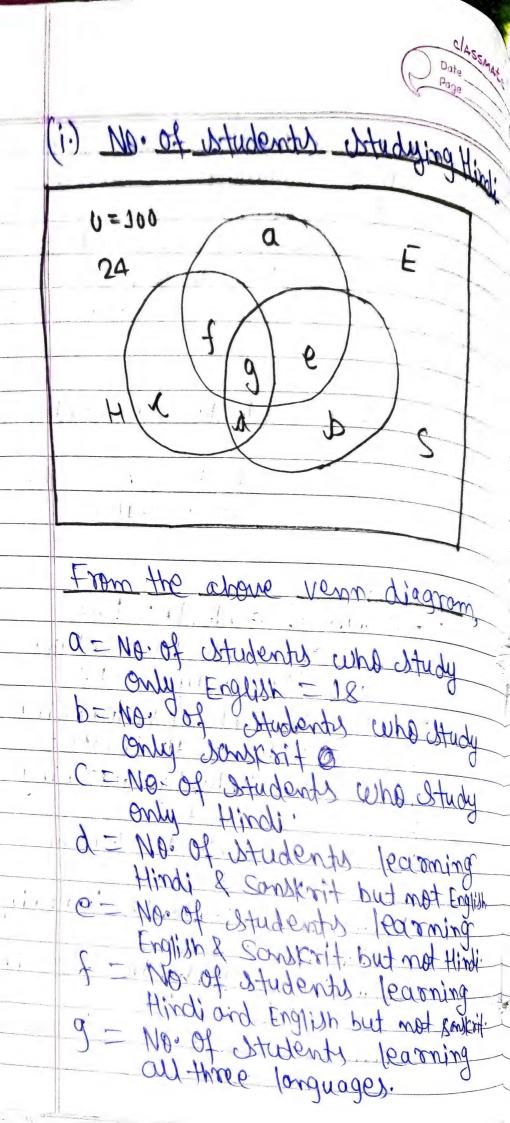
9 - Number of people who read newspaper Hand I but not T

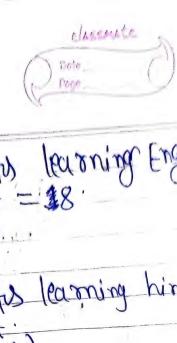
r = Number of people who read newspaper Tord I but not H. 8 = Number of people who read all three newspapers





Q. In a survey of 100 students, the number of students studying the various longuages is found as English only 18; English but not Hindi 23; English and Janskrit 8; Janskrit and Hindi 8; English 26; Sonskrit 48 and no longuage 24. (i) how many students are studying Hindi? (ii) how many students are studying English and Hindi both? dy: Given: - Total mo. of Studenty = 100 - Number of Studenty Studying English (E) only = 18 - Number of Students learning English but mot Hindi (H) = 23 - Number of students learning English & Sanskrit (S) = 8 - Number of Studenty learning - Number of Students learning Emplish = 26: - Number of Students learning Sanskrif = 48 - Number of Students learning one language = 24





6+3= 10. of students learning English = m(ED3)... 9+d = No. of students learning himli and sanskrit = n (Hns) = 8

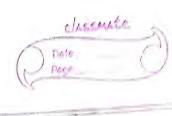
E = 10+e+f+9

= Number of Studenty learning English 26 = 18 + 18 + f $\Rightarrow f = 26 = 26 = 0$ Therefore, f = 0

Number of Studenty learning English
but not Hindi

Naw, 6+9 = 8.

S= b+ e+ d+9 = Number of studenty Studying conskrit. 48 = b+5+8 ("id+g=8) ⇒ b = 48-13. studying sansk sit only also, NAW Number of Students Studying Hirdi Only -1=100- (a+e+b+d+f+g)-24 =100 - (18+5+35+5+0+3)-24= 100 - \$66 - 24 = 300 - 94

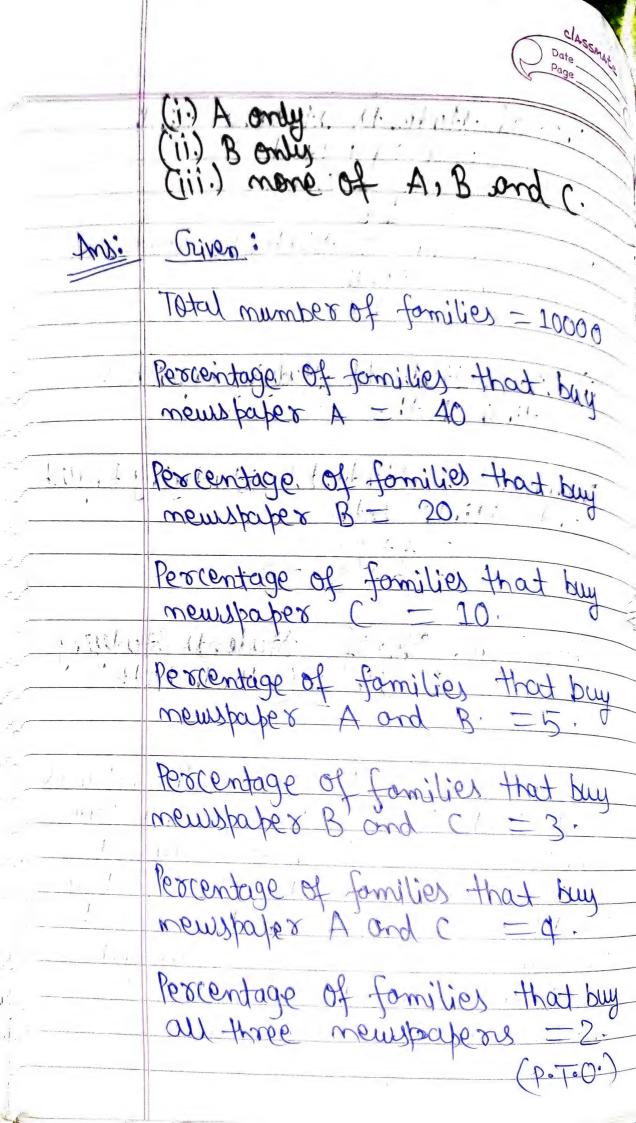


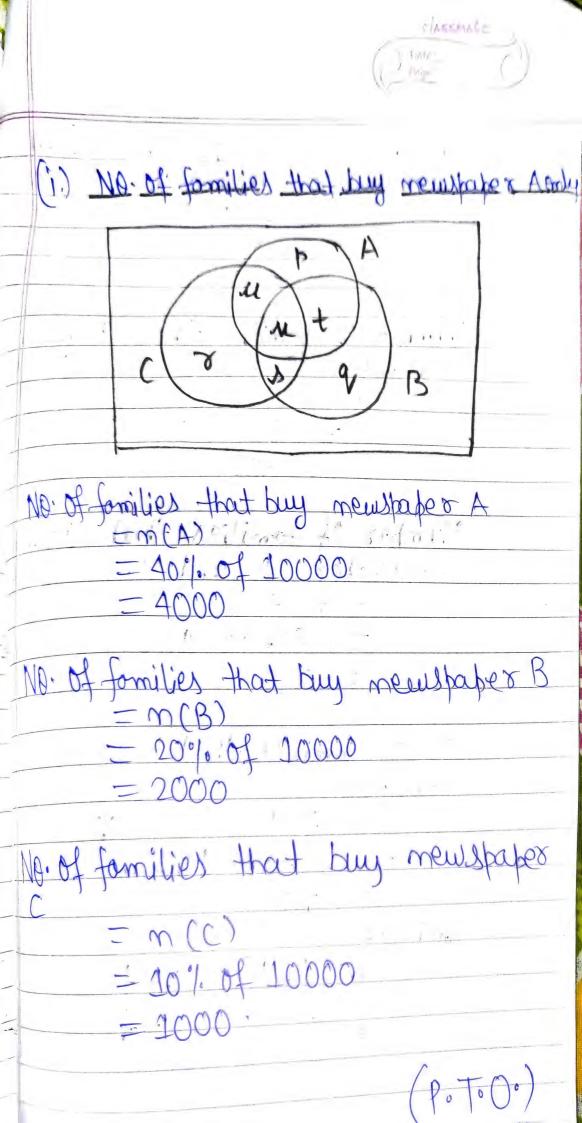
No. of students studying Hirdi = x + f + 9 + d = 10 + 0 + 3 + 5 = 18. Therefore, no. of studenty students.

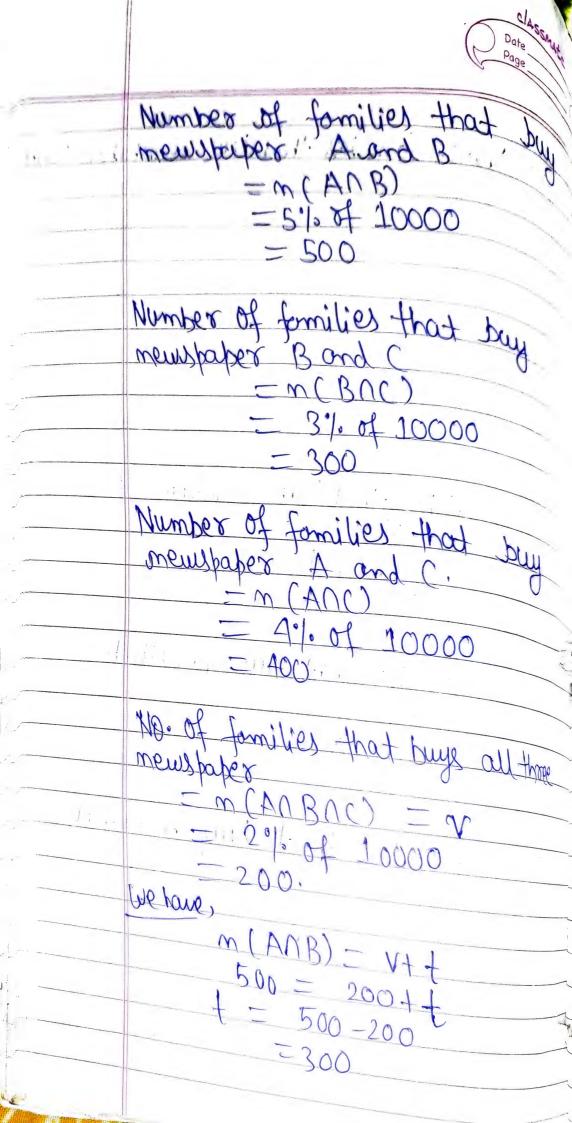
Studying Hindi

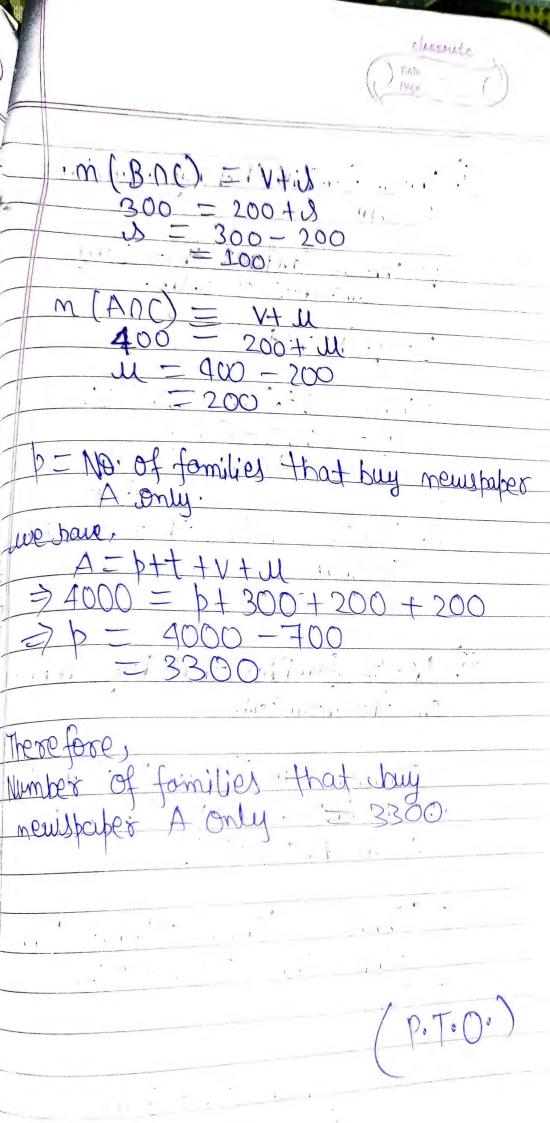
18. (ii) No. of students studying English & Hindi both. Number of Students Studying English and Hindi both Therefore, No. of Students Studying English and Hindi both

= 3. In a four of 10,000 families, it was found that 40 % of the families buy newspaper A, 20% buy newspaper B, 10% buy memspaper C, 5% buy A and B; 3% buy B and C, and 4% buy A and C. If 2% buy all the three newspapens, find the no of families which buy:—











(11) NO. of families that by newstates

9=No. of families that buy newspaper B only.

B=9+0+V+t

2000 = 9 + 100 + 200 + 300 9 - 2000 - 600 = 1400

.. No. of families that newspaper

B only

= 1400

(111-) No. of families that buys mone

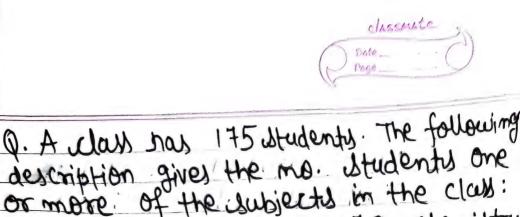
= $10000 - \{m(A) + m(B) + m(C) - m(AnC) - m(AnC)$

+ m(AnBac)}

= 10000 - (4000 + 2000 + 1000 - 500 - 300 - 400 + 200)

= 10000 - 6000 = 4000

.. No. of families that buy mome of newspaper = 4000.



description gives the mo. Students one or more of the subjects in the class: mathematics 100, physics 70, chemistry 46, mathematics and physics 30; mathematics and chemistry 28; physics and chemistry 28; mathematics, physics and chemistry 18.

Find:—

i) How many students are enrolled

(i) How many students are enrolled in Mathematics alone, physics alone and chemistry alone.

- Number of Students in Italian = 175.

- Number of Students envolled in

Mathematics = 100

- Number of Students envolled in

Physics = 70

- Number of Students enrolled in Chemistry = 46. - Number of Students enrolled

in Mathematics and Physics = 30.

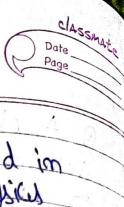
- Number of Students enrolled

in Physics and Chemistry = 23.

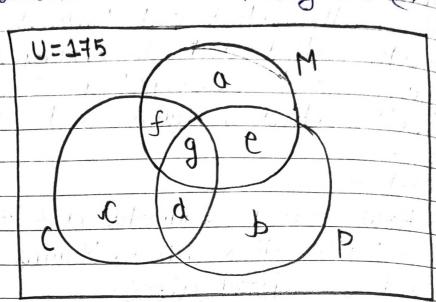
- Number of Students enrolled in

Mathematics and Physics = 28.

- No. of Students enrolled in all three subjects = 18.



No. of students empled in Mathematics alone, Physics alone and chemistry alone.



No. of Students enrolled in

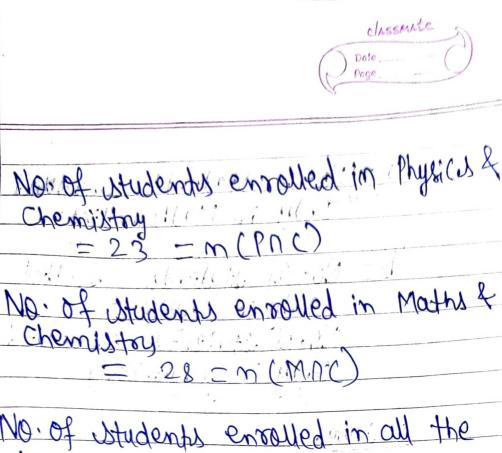
of the man of the device of the control of the cont

Physics = 70

No. of Students enrolled in Chemistry = 76

No of students envolled in Moths

2 Physics - MMP).



Chemistry = 28 = m (MAC)

No of students enrolled in all the three subjects 18 = m: (MAPAC) = 9

we have,

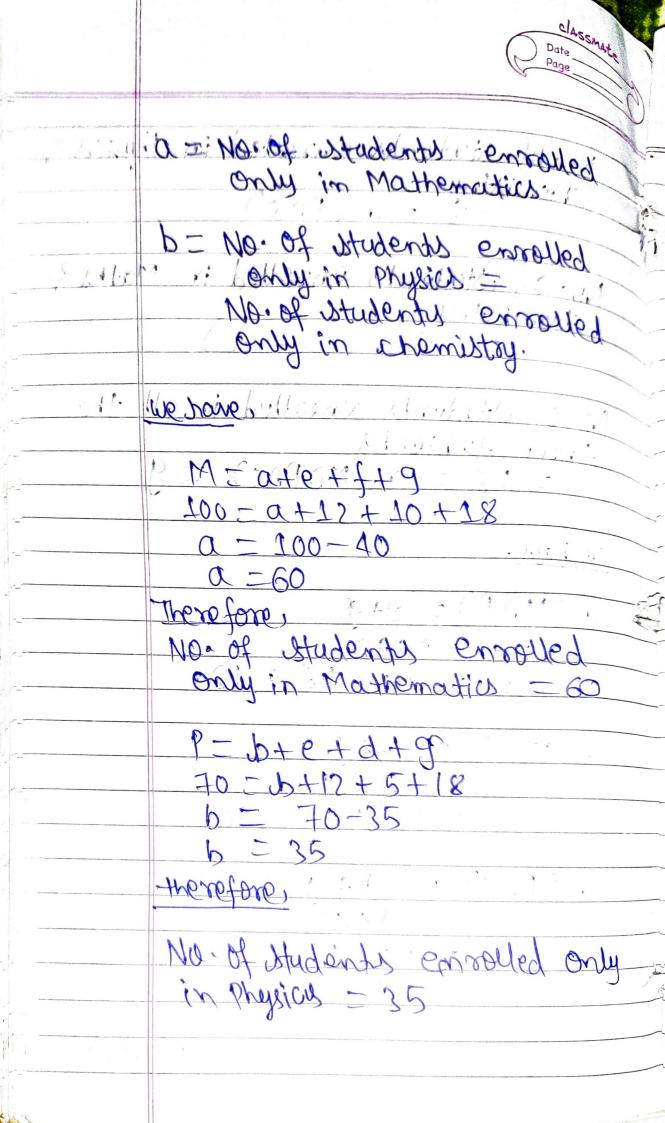
m(MnP) = e+g

M(MNC) = f+9. f = 28-18 = 10.

M(PNC) = d+9 23 = d+18d=23-18

=5.

(PoToOo)



CINSMILE S

C = 24f + d + 9 46 = 2410 + 5 + 18 2 = 46 - 33 = 13Therefore,

No of estudents enough only in Chemistry = 13.

(ii.) Number of Students who have most offered any of these subjects.

= 175-{n(M)+n(P)+n(c)-n(M)P)}
-n(M)C)- m(P)C)+n(M)P)C)

= 175-(100 +70 +46-30-28-23+18)

=175-153 =22.

Therefore,

Number of Students who have not offered any of these subjects

= 27.